

GATE 2024



प्रचण्ड Batch

HMT

MODES OF HEAT TRANSFER

TIME- 4:30PM

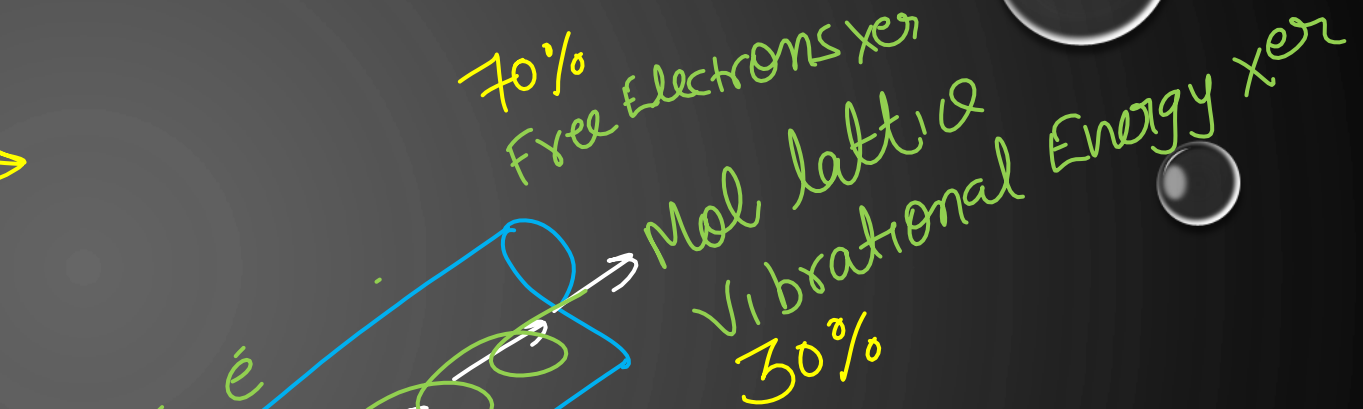
YOGESH SIR



Modes of Heat transfer →

- ① Conduction
- ② Convection
- ③ Radiation

Conduction →



Solid which is good conductor of Electricity well Also a good conductor of Heat

Exception → Diamond

$$k_{\text{Diamond}} = 2300 \frac{\text{W}}{\text{m}\cdot\text{K}}$$

Conduction

30%

Mol lattice Vibrational
Energy xer



Phononic Conduction

70%

Free Electrons
xer

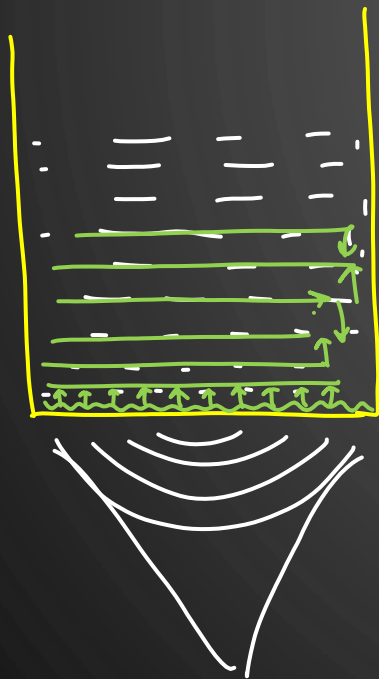


Electronic Conduction



Conduction
is a Micro
scopic
Phenomenon

Conduction in Liquids →



Condⁿ Also occurs in liquids
When high velocity high temp
Molecule comes in contact with
low vel, low temp mol

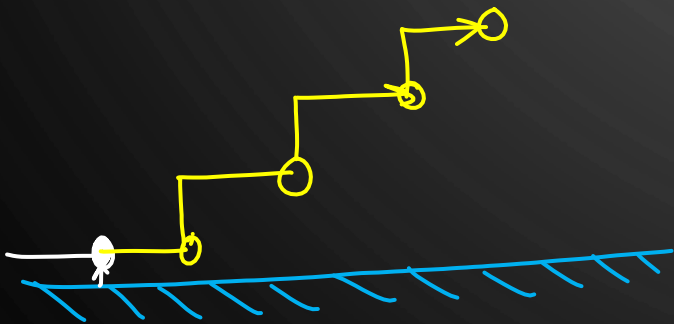
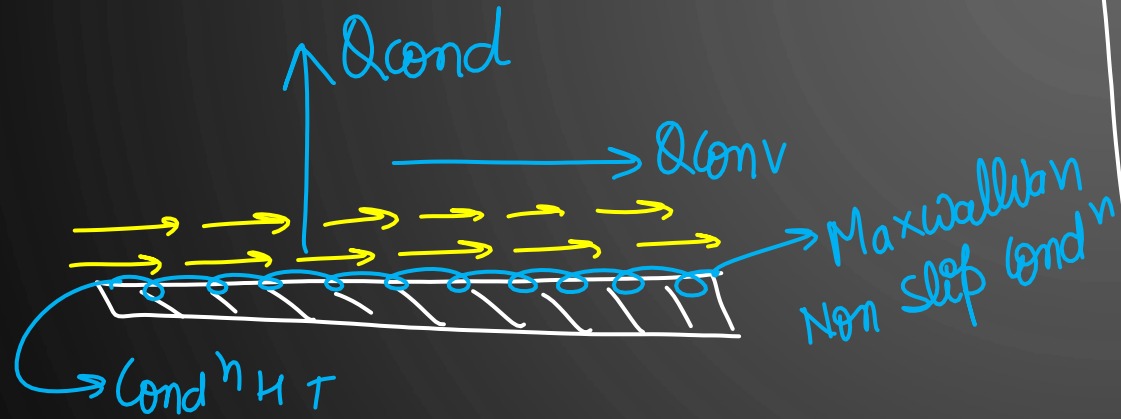
They exchange their heat & this
Phenomenon is known as Condⁿ in
Liquids.

xxx



High vel & High Temp Mol collides
with Low vel Low temp mol
→ Conduction in Gases.

Convection →

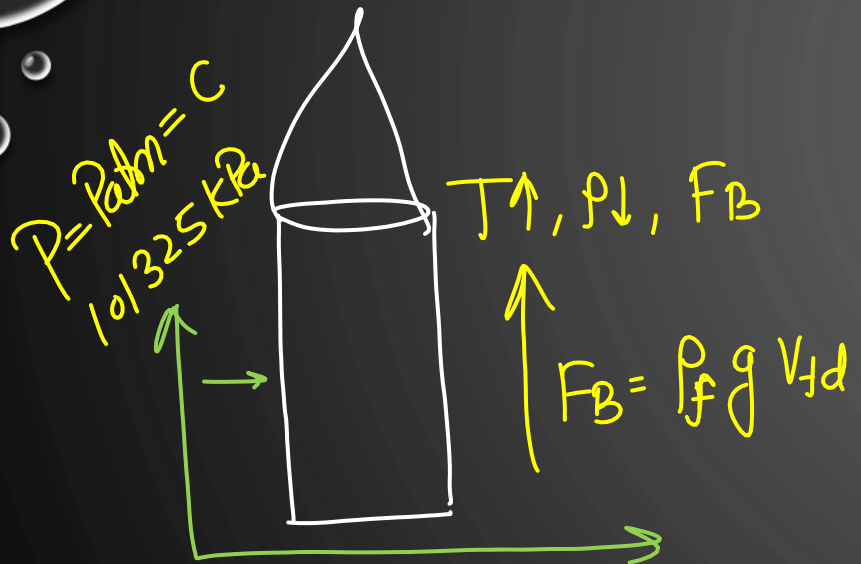


In convection HT, HT by $Cond^n$ is Transported by fluid (flowing)

* Convection is a Transport Phenomenon.

Convection





$$PV = nRT$$

$$P = \frac{n}{V} RT$$

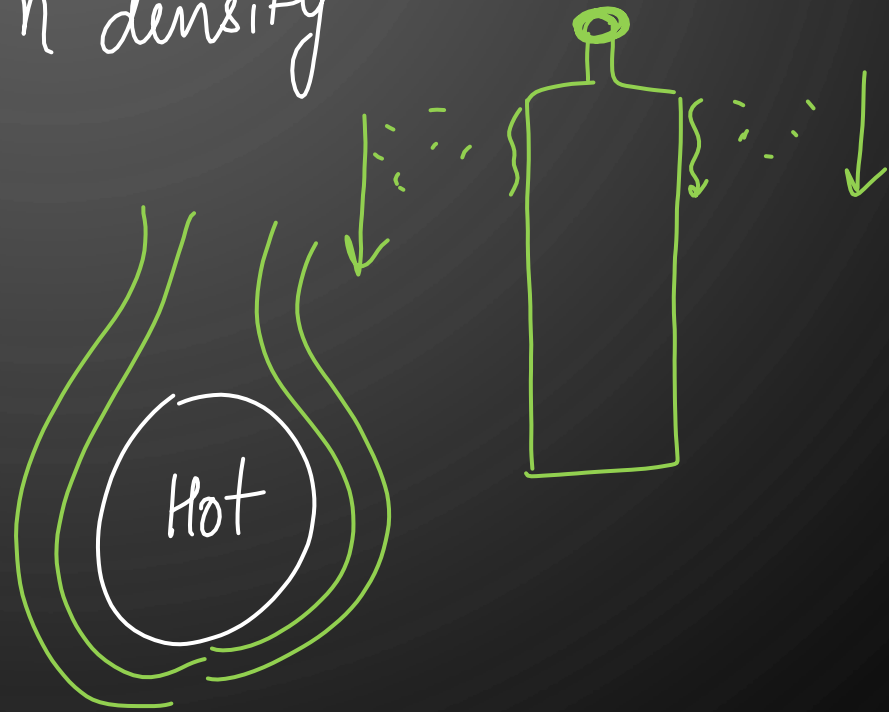
$$P = \rho RT$$

$$\rho \propto \frac{1}{T}$$

$$T \uparrow, \rho \downarrow$$

$$T \downarrow, \rho \uparrow$$

If the Flow takes place Naturally due
 density Density Difference i.e. due to
 Buoyancy Forces arising by change
 in density





When convection $H \cdot T$
Takes place with the help
of some external Agent
i.e. forcefully then it
is known as forced convection.

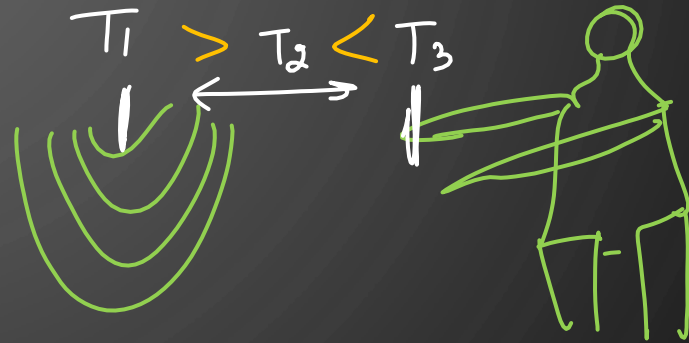


Bulk Displacement of fluids forced
→ Macroscopic phenomenon

Radiation →

Radiation is the Mode of HT which do not require Any Material, ^{medium} and hence Radiation Heat Transfer take place with the help of EMT, wave Propagation, which Travel with the speed of light.

Radiation HT Dominates over Conduction & Convection when temp diff is very high



All bodies at All temperatures emit thermal Radiation except the body is a 0K
at 0K → Mol Become Motionless

Steady State Conduction-1

4:30 PM

Note: → Liquids are better conductor of heat as compare to gases

$$k_{\text{water}} = \overset{0.61}{\cancel{0.69}} \text{ W/m-k}$$

$$k_{\text{Air}} = 0.023 \text{ W/m-k}$$

Governing law for Condⁿ

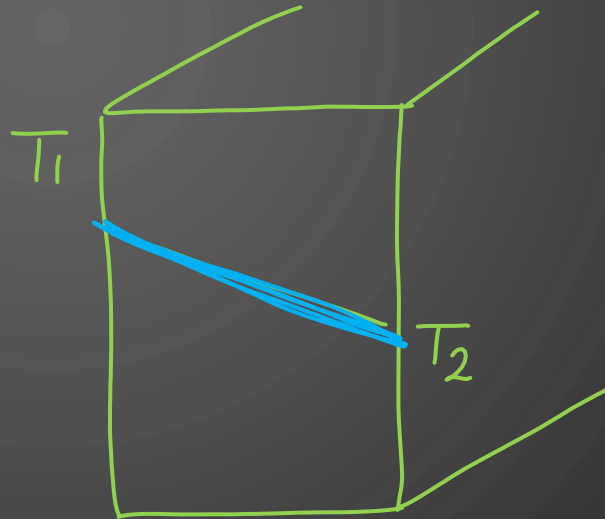
Fourier law of conduction H.T.

→ B/W two Isothermal Surface

$$\frac{dT}{dy} = 0$$

$$\frac{dT}{dz} \neq 0$$

$$\frac{dT}{dt} = 0$$



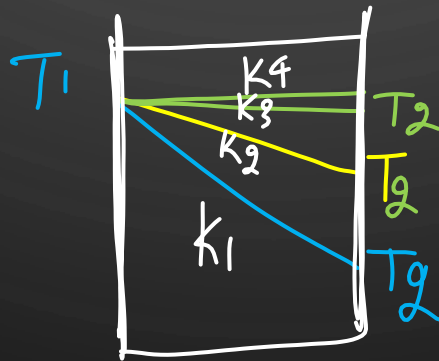
$$Q = -kA \frac{dT}{dx}$$

$$k = \frac{Q}{-A \left(\frac{dT}{dx} \right)}, \quad A=1, \frac{dT}{dx}=1, \quad \boxed{k=Q}$$

$$K = Q$$

* Conductivity defined as the Rate of HT Per unit Area, Per unit temp Gradient, (in the Dir'n of Motion), b/w two Isothermal Walls

* It is thermophysical Property of Material which Allows the heat to get conducted through it



$$k_4 > k_3 > k_2 > k_1$$

Metals →

$K_{\text{Silver}} \rightarrow 405 \text{ W/m-k}$

$K_{\text{Copper}} \rightarrow 385 \text{ W/m-k}$

$K_{\text{gold}} \rightarrow 260 \text{ W/m-k}$

$K_{\text{Al}} \rightarrow 205 \text{ W/m-k}$

$K_{\text{Iron}} \rightarrow 110 \text{ W/m-k}$

$K_{\text{steel}} \rightarrow 17 \text{ to } 45 \text{ W/m}$

Non-Metal

→ Crystalline (Perfect Crystalline Structure)

→ Amorphous

$K_{\text{glass}} = 1.5 \frac{\text{W}}{\text{m-k}}$

→ $K_{\text{Diamond}} = 2300 \text{ W/m-k}$

→ $K_{\text{graphite}} = 1100 \text{ W/m-k}$

→ $K_{\text{Copper Crystal}} = 8000 \text{ W/m-k}$

Material which have low thermal conductivity
are known as Insulators → used to Prevent Rate of HT

$$K_{\text{Asbestos}} = 0.2 \text{ W/m-k}$$

$$\text{PUF} / K_{\text{glass wool}} = 0.032 \text{ W/m-k}$$

↳ Poly urethane foam

$$K_{\text{refractory Bricks}} = 0.9$$

$$K_{\text{freon Gas}} = 0.0083 \text{ W/m-k}$$

$$K_{\text{metals}} > K_{\text{liquids}} > K_{\text{gases}}$$

Note-1 K vary with dir'n
4 it does not vary Mater'n
is known as Isotropic



$$K \neq f(x, y, z)$$

Isotropic

Conductivity varies with location in a given dish \rightarrow

$\rightarrow k_1 \rightarrow k_2 \rightarrow k_3 \dots$

\rightarrow heterogeneous material

In General

$$k = f(T, P, \rho, \text{Porosity, Moisture})$$

Solids

Variation of Conductivity in Metals →

$$K = k_0 + k_1 T + k_2 T^2 + k_3 T^3 + \dots$$

$$K = k_0 \left[1 + \frac{k_1}{k_0} T \right] + k_2 T^2 \left[1 + \frac{k_3}{k_2} T \right] + \dots$$

$$K = k_0 [1 + \alpha T]$$

$\alpha \rightarrow$ Constt

$\alpha \rightarrow$ -ve (Pure Metals)

$\alpha \rightarrow$ +ve (Alloys)

$$K = k_0 (1 - \alpha T), T \uparrow, K \downarrow$$

Pure Metals

$$K = k_0 (1 + \alpha T), T \uparrow, K \uparrow$$

Alloys

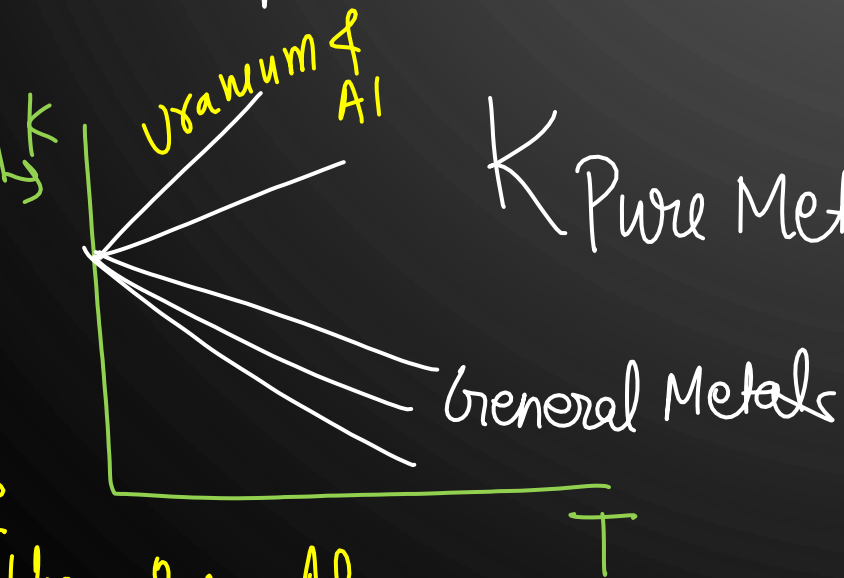


$T \uparrow$, Impurities \downarrow
Purity \uparrow , $K \uparrow$

Pure Metals $\rightarrow T \uparrow, K \downarrow, \alpha (-ve)$

Alloys $\rightarrow T \uparrow, \text{Impurities} \downarrow, \text{Purity} \uparrow, K \uparrow, \alpha (+ve)$

$$K = f(\text{Purity of Metal})$$



$K_{\text{Pure Metals}} > K_{\text{Alloys}}$

Exp \rightarrow

Uranium, Al

$$K = k_0 (1 \pm \alpha T)$$

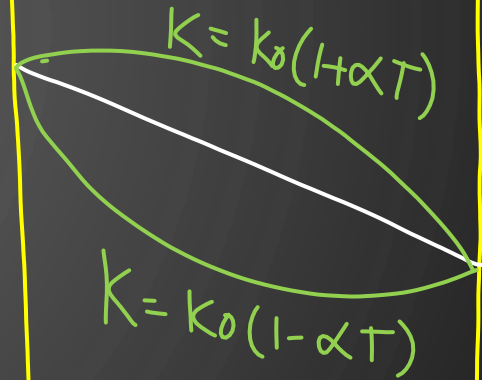
$k_0 \rightarrow K$ at 0°C

$$k_0 = \frac{W}{m^\circ\text{C}}$$

$T \rightarrow ^\circ\text{C}$

$$\alpha \rightarrow \frac{1}{K} \propto \frac{1}{\alpha}$$

$$K_{\text{Metals}} = f(T)$$



K vary linearly

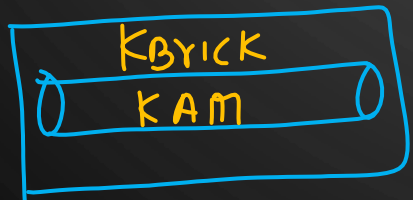
$$K = \frac{K_1 + K_2}{2}$$

Non-Metallic Solids →

$$K = (\text{Porosity, Moisture Content})$$

Porosity ↑, K ↓, $K \propto 1/\text{Porosity}$

Moisture ↑, K ↑, $K \propto \text{Moisture}$.



$K_{avg} \downarrow$, Rate of HT ↓

↳ Red Brick
(More Moisture)

→ Refractory Bricks

$$\underline{K_{\text{Red Bricks}} > K_{\text{Refractory Bricks}}}$$