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Achieve"  
So start thinking..*

*Renu Raj Garg  
M.Tech (VLSI Design)  
13 Year of Teaching  
Experience  
Worked 10 Year in NTRO*



# GATE 2024



**प्रचण्ड** Batch

## COMMUNICATION

### QUESTIONS FROM QUANTIZER

TIME- 9:00PM

RENU SIR





Chapter-2

**Digital Communications**

*In today's lecture we will cover the following Topics :*

1. *Questions from Quantizer in PCM*





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# GATE 2023 RESULT



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<b>AIR</b> <b>64</b> <b>CE</b> UTKARSH MISHRA	<b>AIR</b> <b>71</b> <b>EE</b> SOMESH SANJAY PAWAR	<b>AIR</b> <b>76</b> <b>CE</b> DIPANKAR DAS	<b>AIR</b> <b>87</b> <b>EC</b> SURAJIT RABI DAS	<b>AIR</b> <b>91</b> <b>EE</b> RISHABH GUPTA	<b>AIR</b> <b>111</b> <b>ES</b> ANIL GUPTA
<b>AIR</b> <b>130</b> <b>EE</b> SAURAV PATEL	<b>AIR</b> <b>136</b> <b>CE</b> RUPESH SACHDEVA	<b>AIR</b> <b>200</b> <b>ECE</b> WASIUZZAMA	<b>AIR</b> <b>212</b> <b>IN</b> WASIUZZAMA	<b>AIR</b> <b>217</b> <b>ME</b> VISHAL KUMAR	<b>AIR</b> <b>219</b> <b>ME</b> NITISH KUMAR
<b>AIR</b> <b>258</b> <b>EE</b> MANAV	<b>AIR</b> <b>348</b> <b>EE</b> AMAN NAMDEV	<b>AIR</b> <b>392</b> <b>EE</b> GAURAV MAHAJAN	<b>AIR</b> <b>403</b> <b>EC</b> MOHAN KUMAR SINGH	<b>AIR</b> <b>567</b> <b>EE</b> SHANKAR JHA	<b>AIR</b> <b>571</b> <b>ME</b> VUENDER MEENA





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ELECTRICAL,  
ELECTRONICS COMMUNICATION ENGINEERING

## GATE 2024 & ALL PSU's



Start Apr 11, 2023

7:30 AM to 11:30 PM



# You **Tube** Classes Schedule



## EE & EC ENGINEERING

EXAM TARGET	SUBJECT	TIME	FACULTY
ALL PSUs	ENGINEERING MATHS	11:00 AM	ANANT SIR
GATE 2024-25	NETWORK THEORY	6:00 PM	RAVI SIR
GATE 2024-25	ELECTRICAL MACHINE	7:30 PM	SANTAN SIR
GATE 2024-25	COMMUNICATION	9:00 PM	RENU SIR



# FREE APP CLASS SCHEDULE



**EE & ECE ENGINEERING**

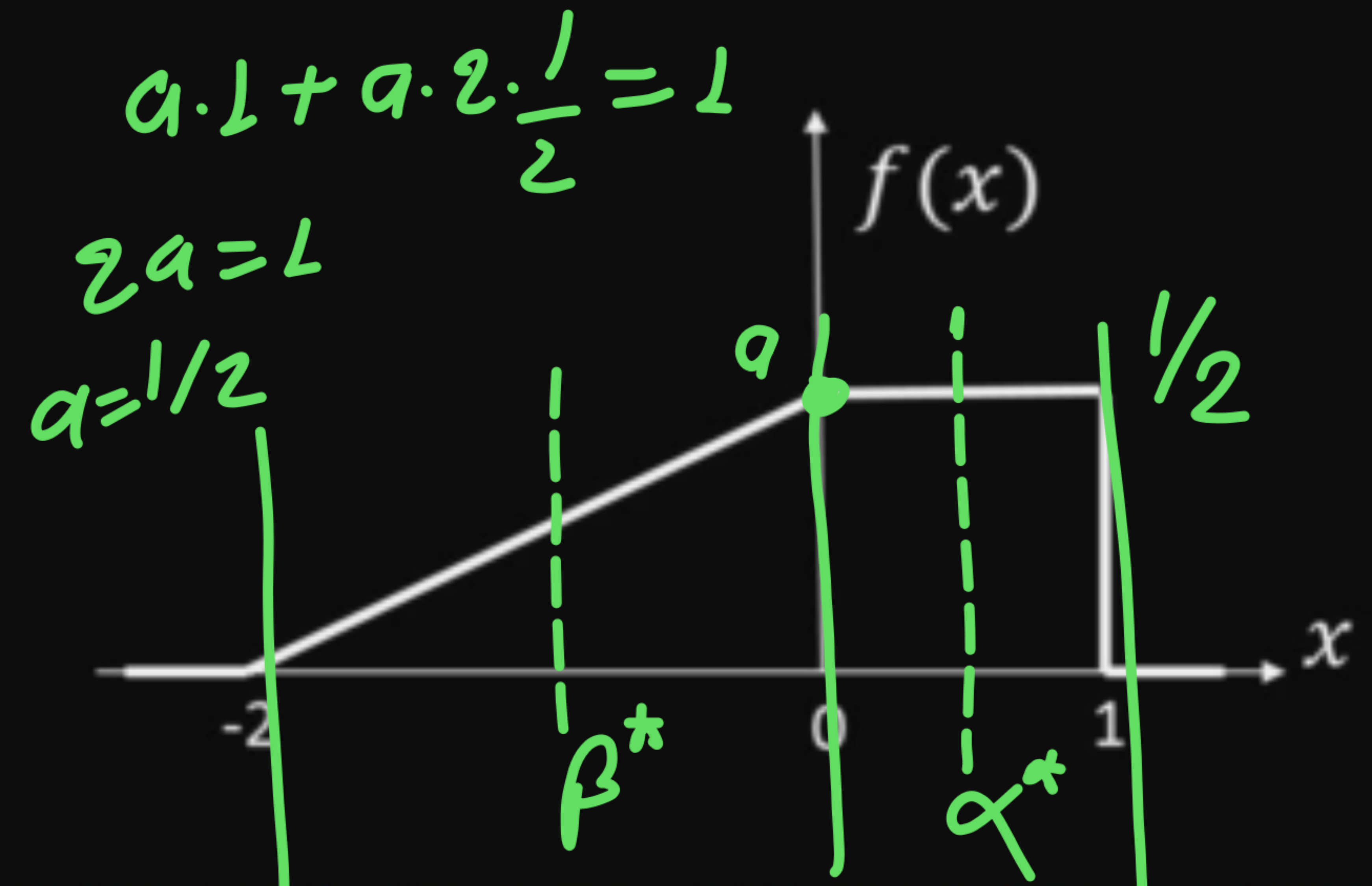


<b>NETWORK THEORY</b>	<b>SATURDAY Live @11AM</b>	<b>RAVI SIR</b>
<b>COMMUNICATION</b>	<b>WEDNESDAY Live @8PM</b>	<b>RENU SIR</b>
<b>ANALOG ELECTRONICS</b>	<b>THURSDAY Live @8PM</b>	<b>LAWRENCE SIR</b>
<b>ENGINEERING MATHEMATICS</b>	<b>FRIDAY Live @11AM</b>	<b>ANANT SIR</b>
<b>ELECTRICAL MACHINE</b>	<b>MONDAY Live @8PM</b>	<b>SANTAN SIR</b>



Consider a real valued source whose samples are independent and identically distributed random variables with the probability density function,  $f(x)$ , as shown in the figure.

GATE-22



Consider a 1 bit quantizer that maps positive samples to value  $\alpha$  and others to value  $\beta$ . If  $\alpha^*$  and  $\beta^*$  are the respective choices for  $\alpha$  and  $\beta$  that minimize the mean square quantization error, then  $(\alpha^* - \beta^*) =$  \_\_\_\_\_ (rounded off to two decimal places).



$$\alpha^* = \frac{0+1}{2} = \frac{1}{2}$$

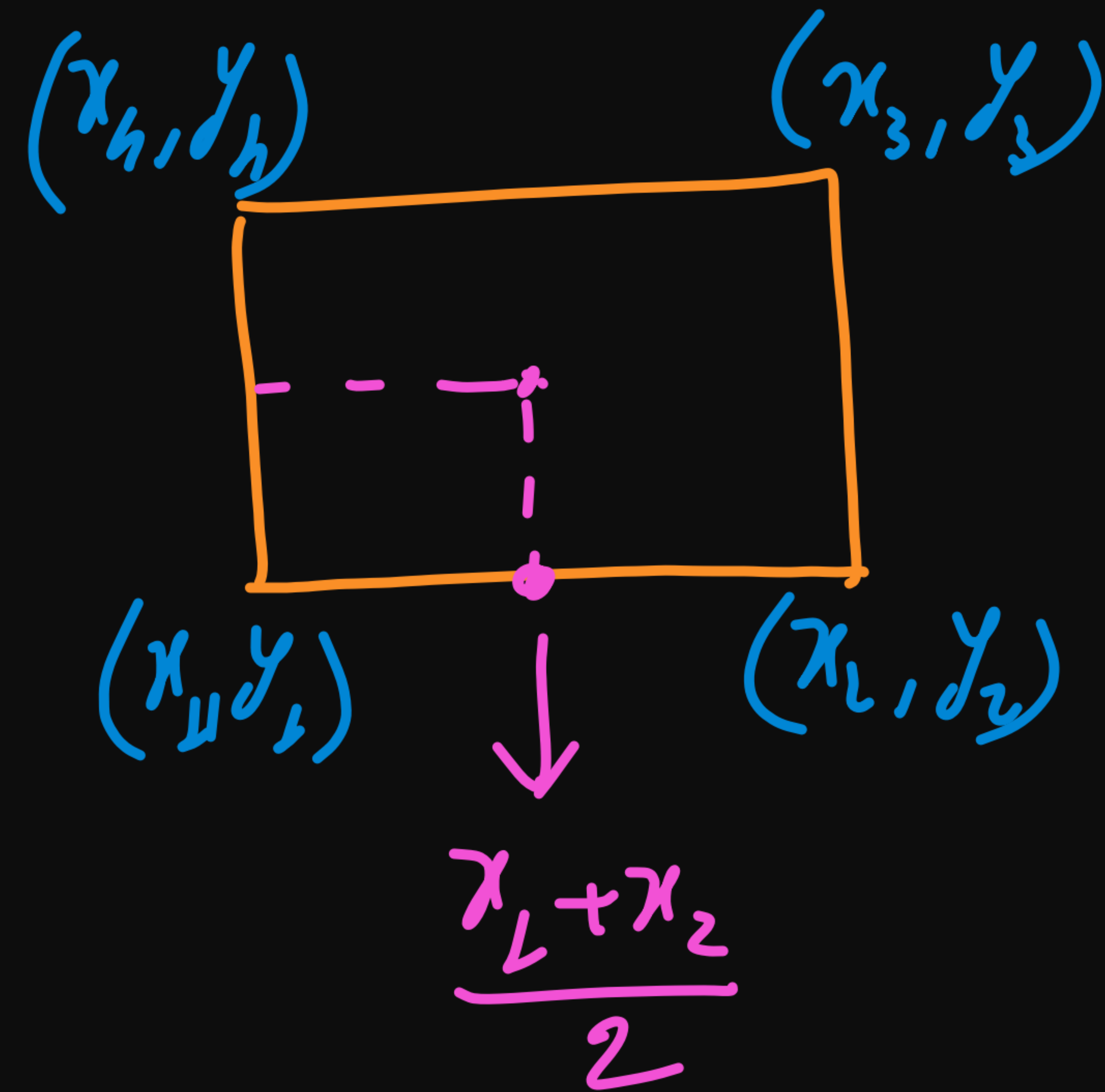
$$\beta^* = \frac{\int_{-2}^0 x f(x) dx}{\int_{-2}^0 f(x) dx} = (\text{centroid})$$

$$\beta^* = \frac{0+0-2}{3} = -\frac{2}{3}$$

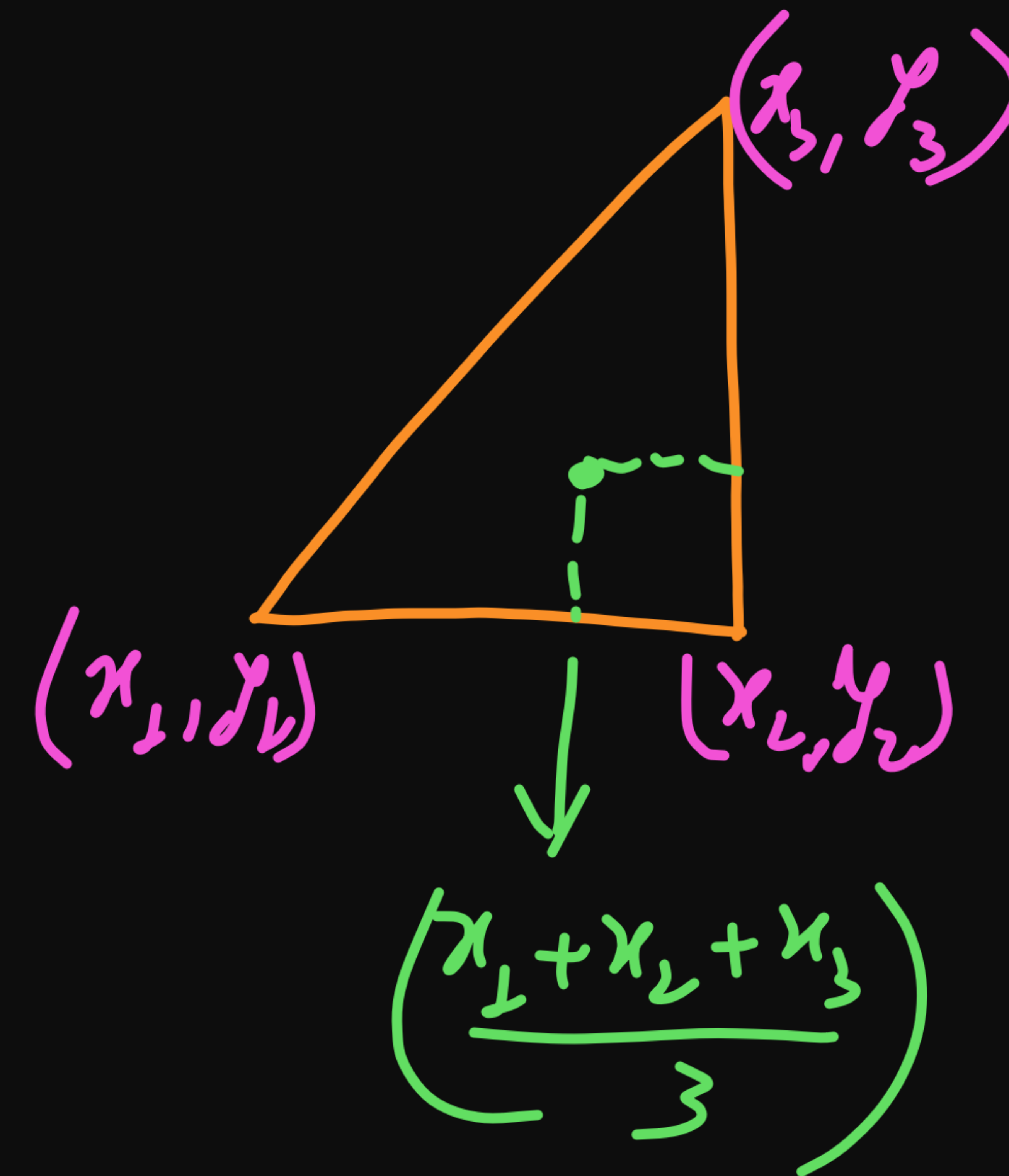
$$\alpha^* - \beta^* = \frac{1}{2} - \left(-\frac{2}{3}\right) = \frac{1}{2} + \frac{2}{3} = \frac{7}{6}$$



### Centroid of Rectangle:



### Centroid of triangle



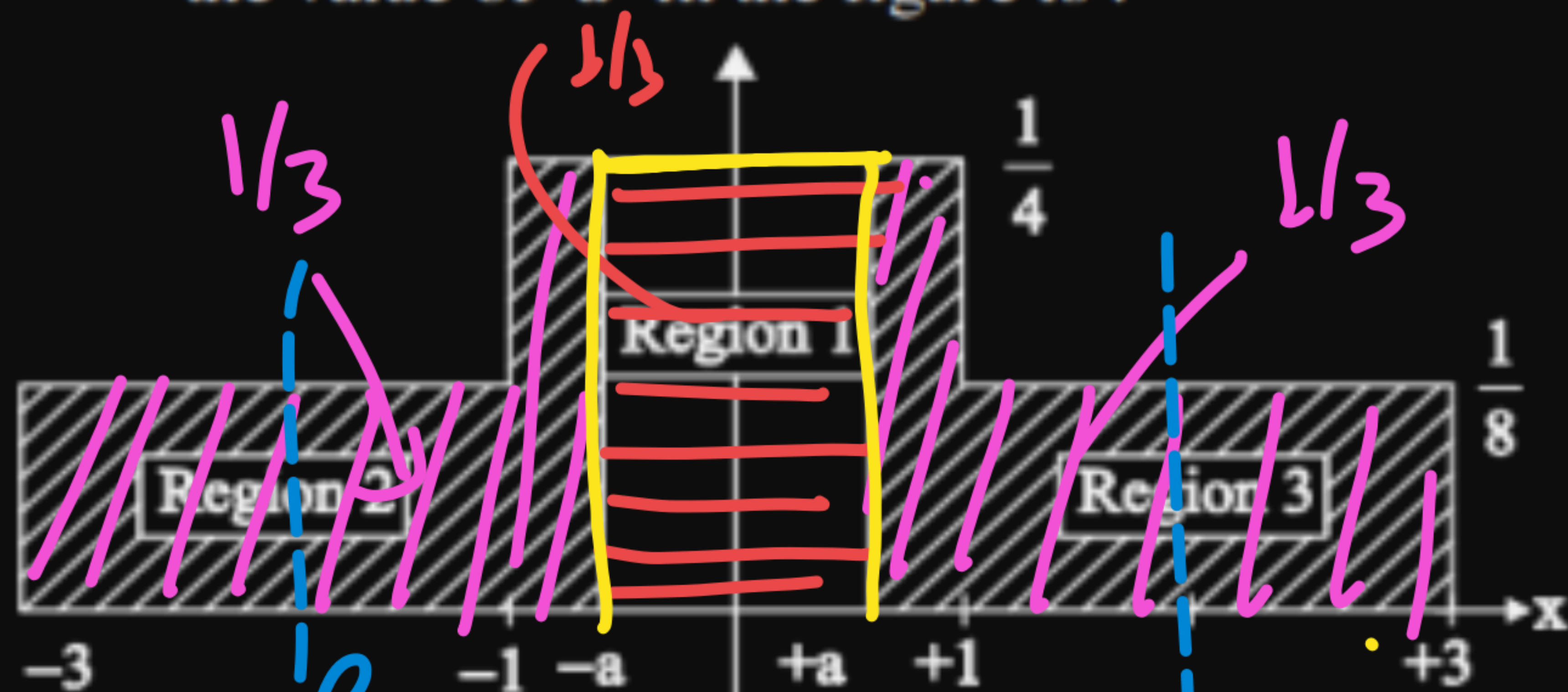


Common Data for the Next Two Questions :

A symmetric three-level midtread quantizer is to be designed assuming equiprobable occurrence of all quantization levels.

[GATE - EC - 2005]

47. If the input probability density function is divided into three regions as shown in figure, the value of 'a' in the figure is :



(A)  $\frac{1}{3}$

(B)  $\frac{2}{3}$

(C)  $\frac{1}{2}$

(D)  $\frac{1}{4}$

[GATE - EC - 2005]

48. The quantization noise power for the quantization region between  $-a$  and  $+a$  in the figure is :

~~(A)  $\frac{4}{81}$~~

(B)  $\frac{1}{9}$

(C)  $\frac{5}{81}$

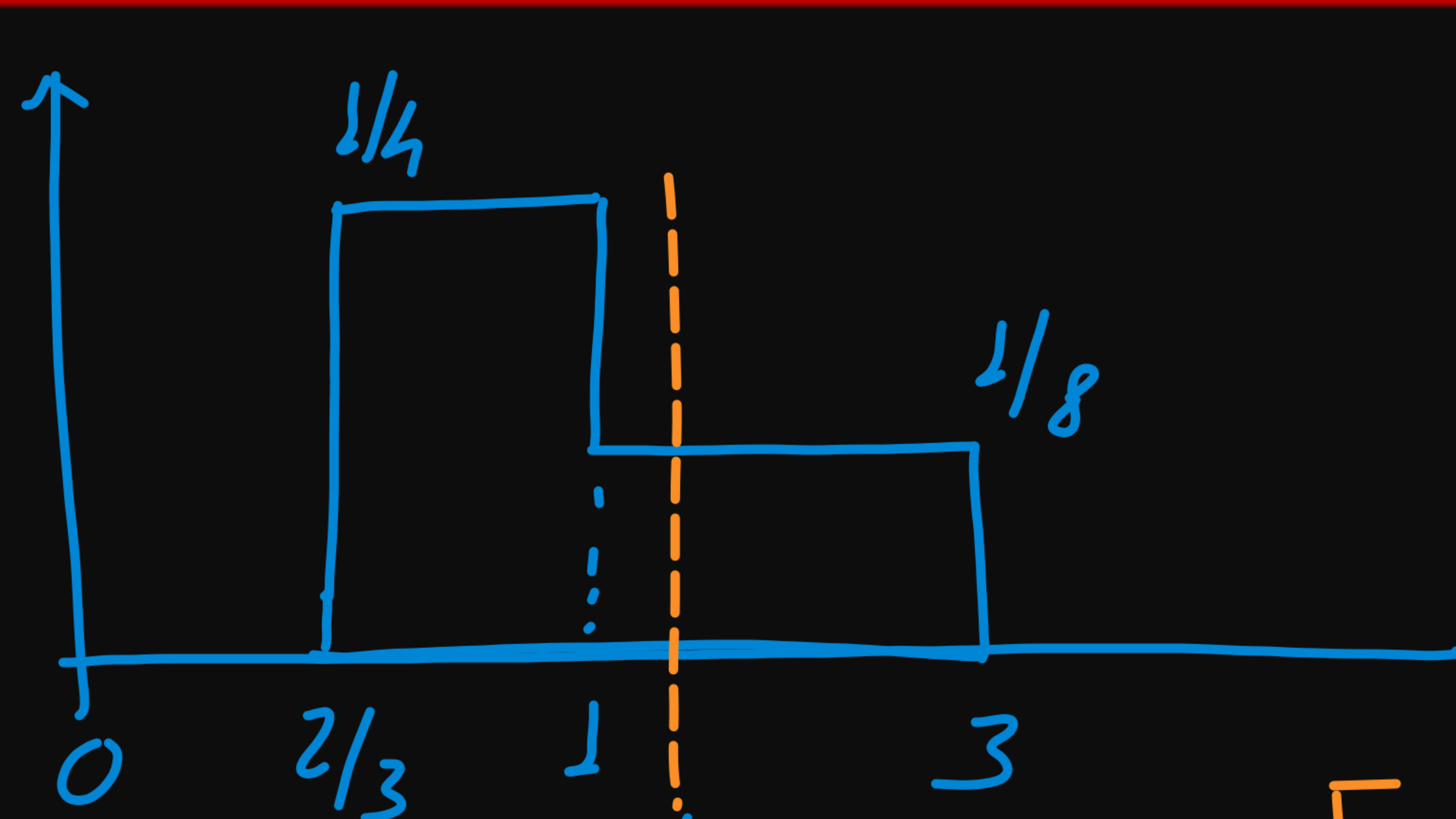
(D)  $\frac{2}{81}$

47  $2a \times \frac{1}{4} = \frac{1}{3}$   
 $9 = \frac{2}{3}$

+3  
 $\frac{2}{3} = +9$   
 $-\frac{2}{3} = -9$   
 $-3$   
 ? = Centroid =  $\frac{2 - \frac{2}{3}}{2} = 0$   
 ? = Centroid =  $\beta = -\frac{41}{24}$

Noise Power (-a to +a)  
 $= \frac{\Delta^2}{12} \times \text{Avg } q$   
 $= \frac{(4/3)^2}{12} \times \frac{1}{3}$   
 $= \frac{16}{12} \times \frac{1}{27} = \frac{4}{81}$

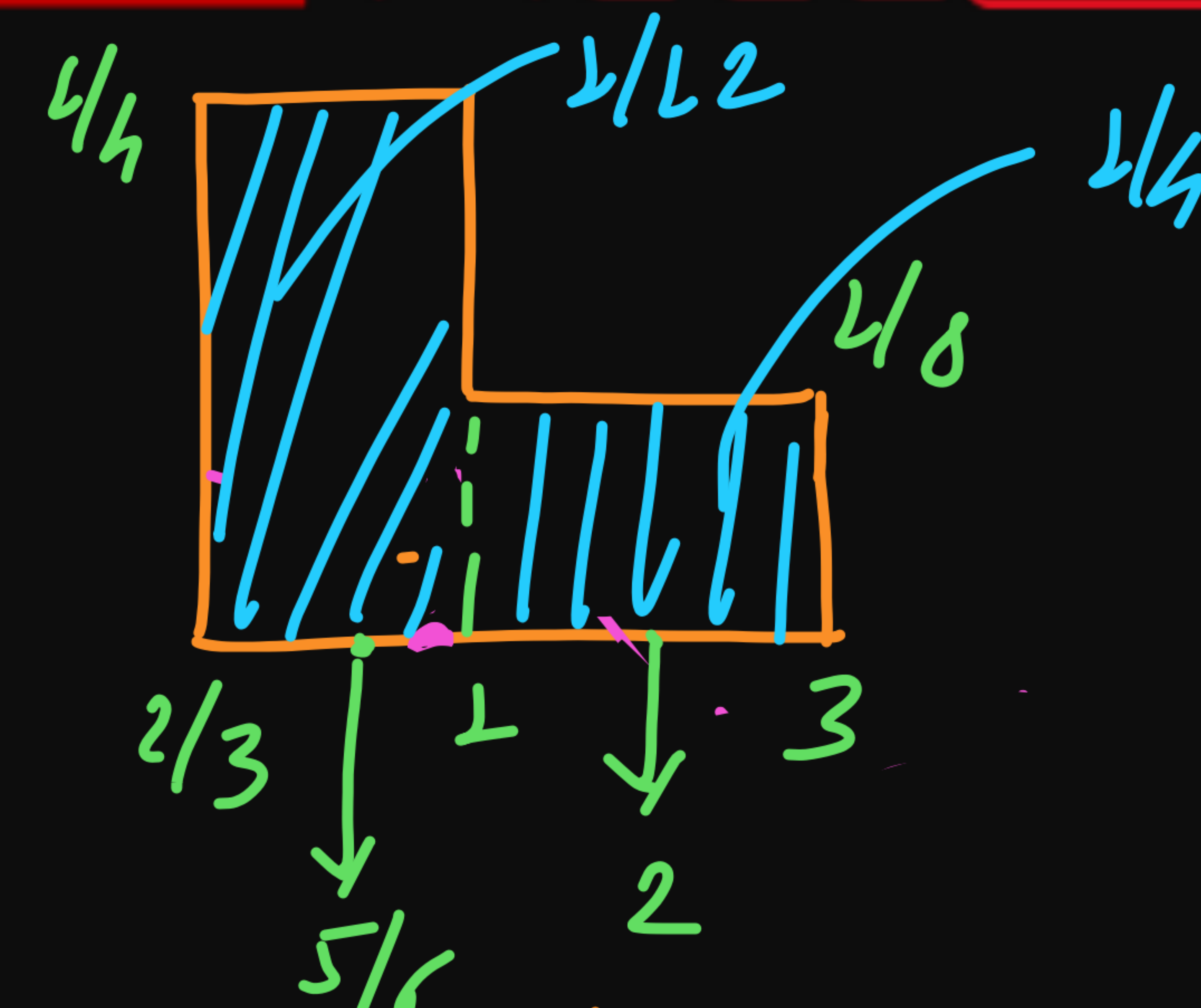




$$\frac{1 + \frac{2}{3}}{2} = \frac{5/3}{2} = \frac{5}{6}$$

$$\frac{1}{3} \times \frac{1}{4}$$

$$\alpha = 1.708 = \frac{5}{24} + \frac{3 \times 11}{2 \times 12} = \frac{41}{24}$$



$$\alpha = \frac{\frac{5}{8} \times \frac{1}{12} + 2 \times \frac{1}{4}}{\frac{1}{12} + \frac{1}{4}} = 1.708$$

(i)  $\int_{2/3}^3 (x - \alpha) f'(x) dx = 0$

(ii) 
$$\alpha = \frac{\int_{2/3}^3 x f(x) dx}{\int_{2/3}^3 f(x) dx} = \frac{\int_{2/3}^1 x \cdot \frac{1}{4} dx + \int_1^3 x \cdot \frac{1}{8} dx}{1/3}$$

$$= \frac{\frac{1}{4} \times \frac{x^2}{2} \Big|_{2/3}^1 + \frac{1}{8} \frac{x^2}{2} \Big|_1^3}{\frac{1}{12} + \frac{1}{4}} = \frac{\frac{3}{8} \left(1 - \frac{4}{9}\right) + \frac{3}{16} (9 - 1)}{\frac{1}{12} + \frac{1}{4}} = \frac{3}{8} \times \frac{5}{9} + \frac{3}{2}$$



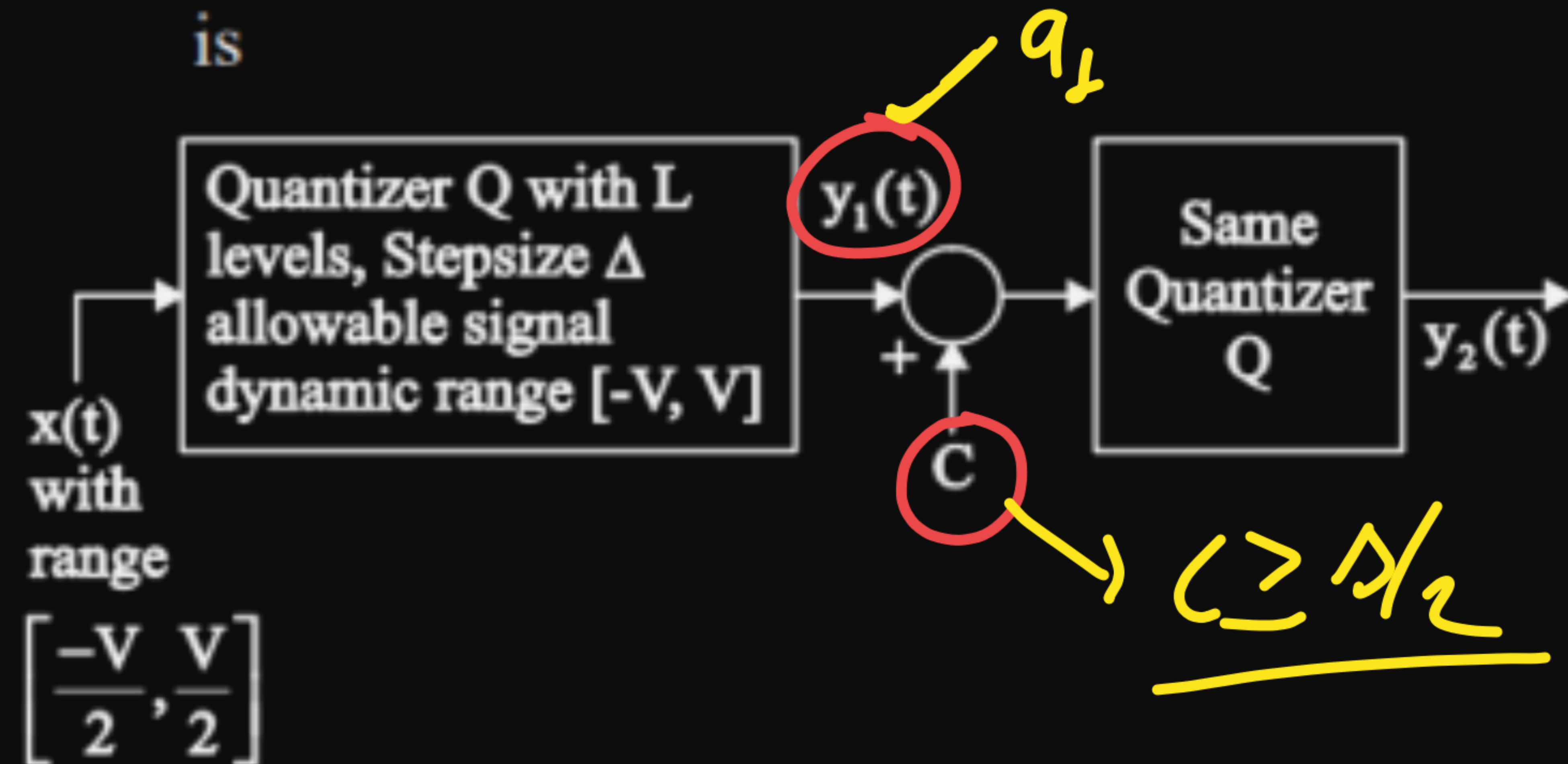
Quantisation noise power for  $+a$  to  $3$ .

$$\begin{aligned} \text{M.P.} \Big|_{+a \text{ to } +3} &= \int_{+2/3}^{+3} (x-a)^2 f(x) dx = \int_{+2/3}^{+1} (x-1.708)^2 \cdot \frac{1}{4} dx + \int_{+1}^{+3} (x-1.708)^2 \cdot \frac{1}{8} dx \\ &= \end{aligned}$$

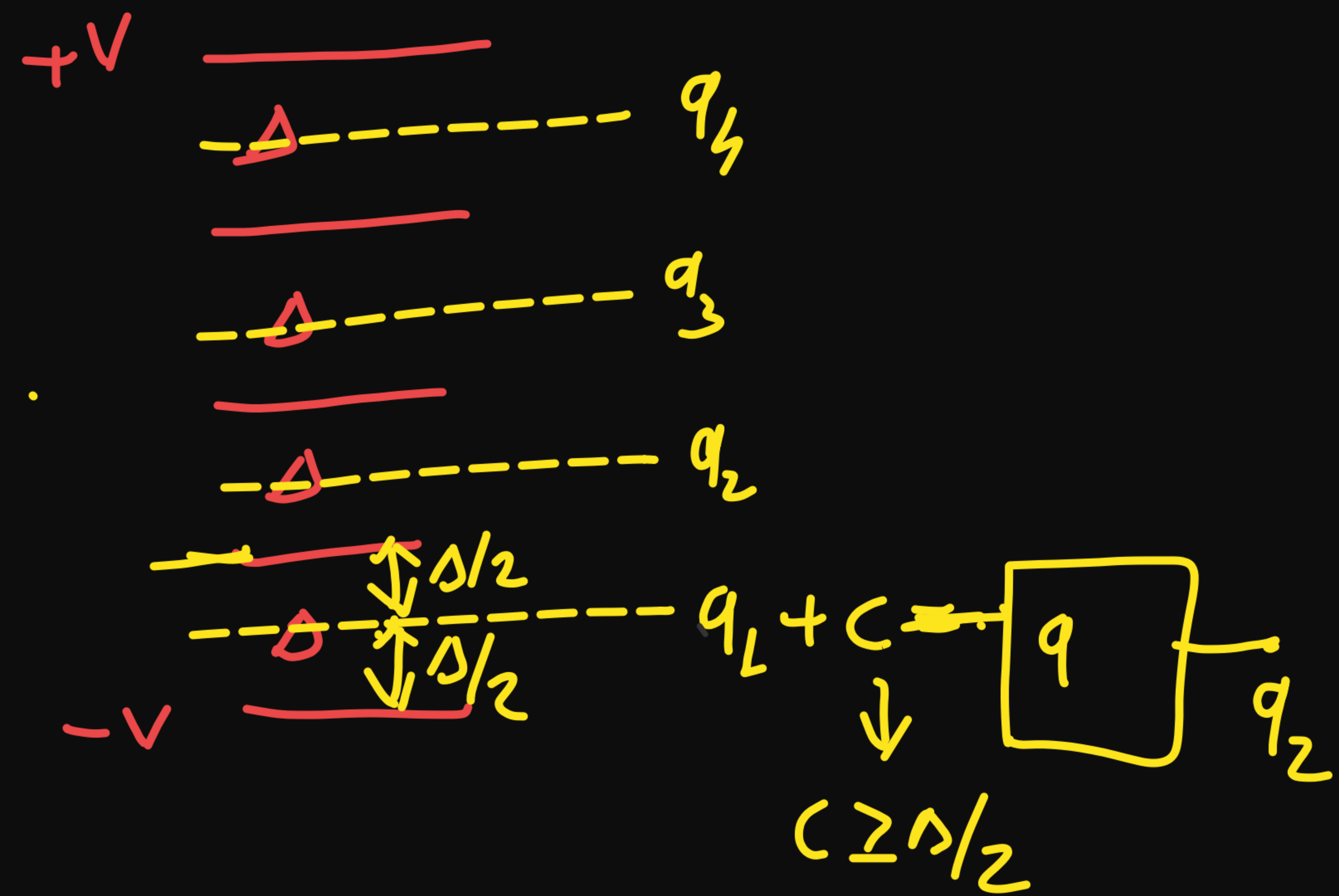


[GATE - EC - 2006]

50. In the following figure the minimum value of the constant "C", which is to be added to  $y_1(t)$  such that  $y_1(t)$  and  $y_2(t)$  are different, is



$V_{max} = +V/2$   
 $V_{min} = -V/2$

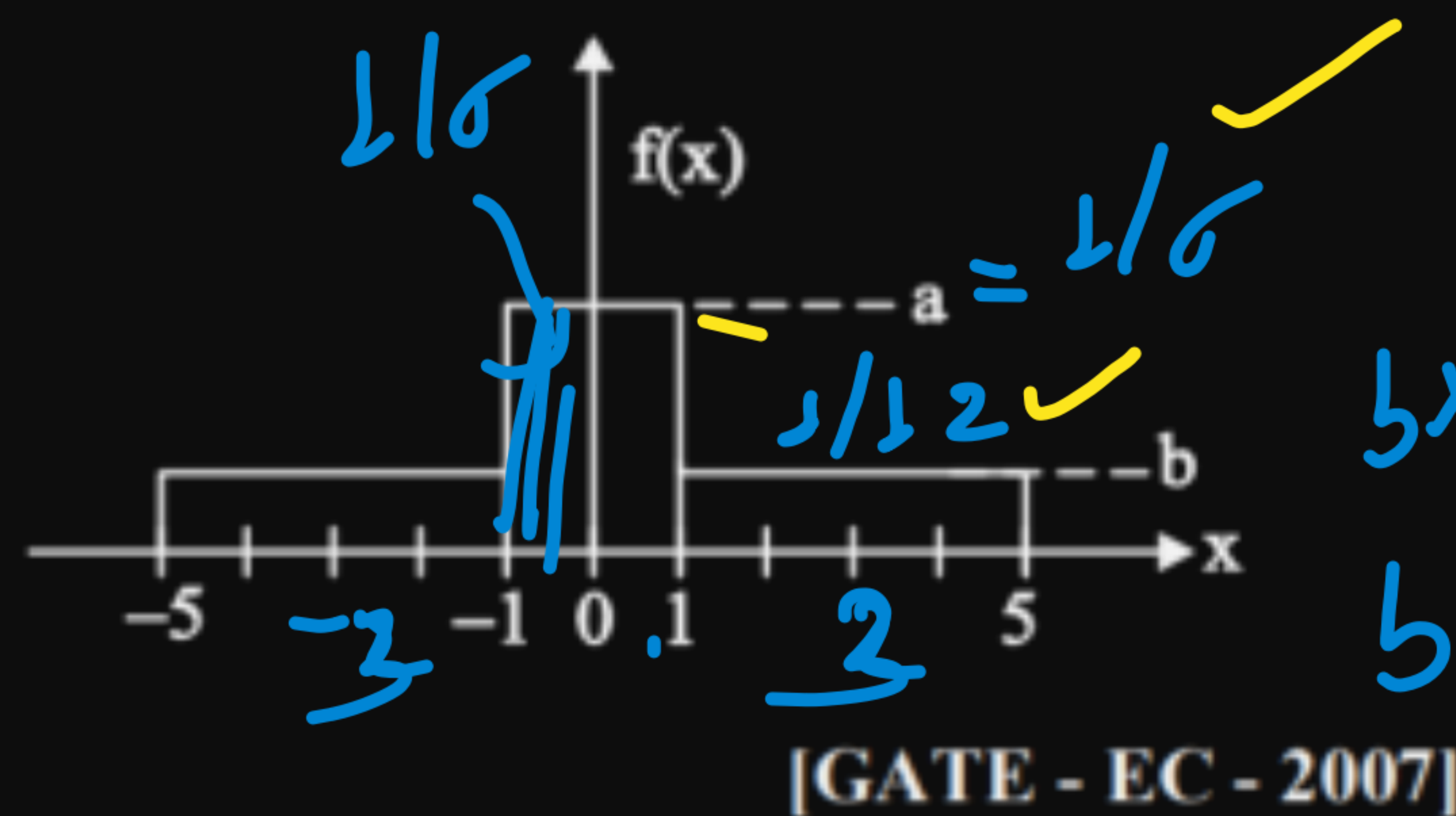


- ~~(A)  $\Delta$~~
- ~~(B)  $\frac{\Delta}{2}$~~
- ~~(C)  $\frac{\Delta^2}{12}$~~
- ~~(D)  $\frac{\Delta}{L}$~~



Statement for Linked Answer Question for Next Two Questions :

An input to a 6-level quantizer has the probability density function  $f(x)$  as shown in the figure. Decision boundaries of the quantizer are chosen so as to maximize the entropy of the quantizer output. It is given that 3 consecutive decision boundaries are '-1', '0' and '1'.



54. The values of a and b are

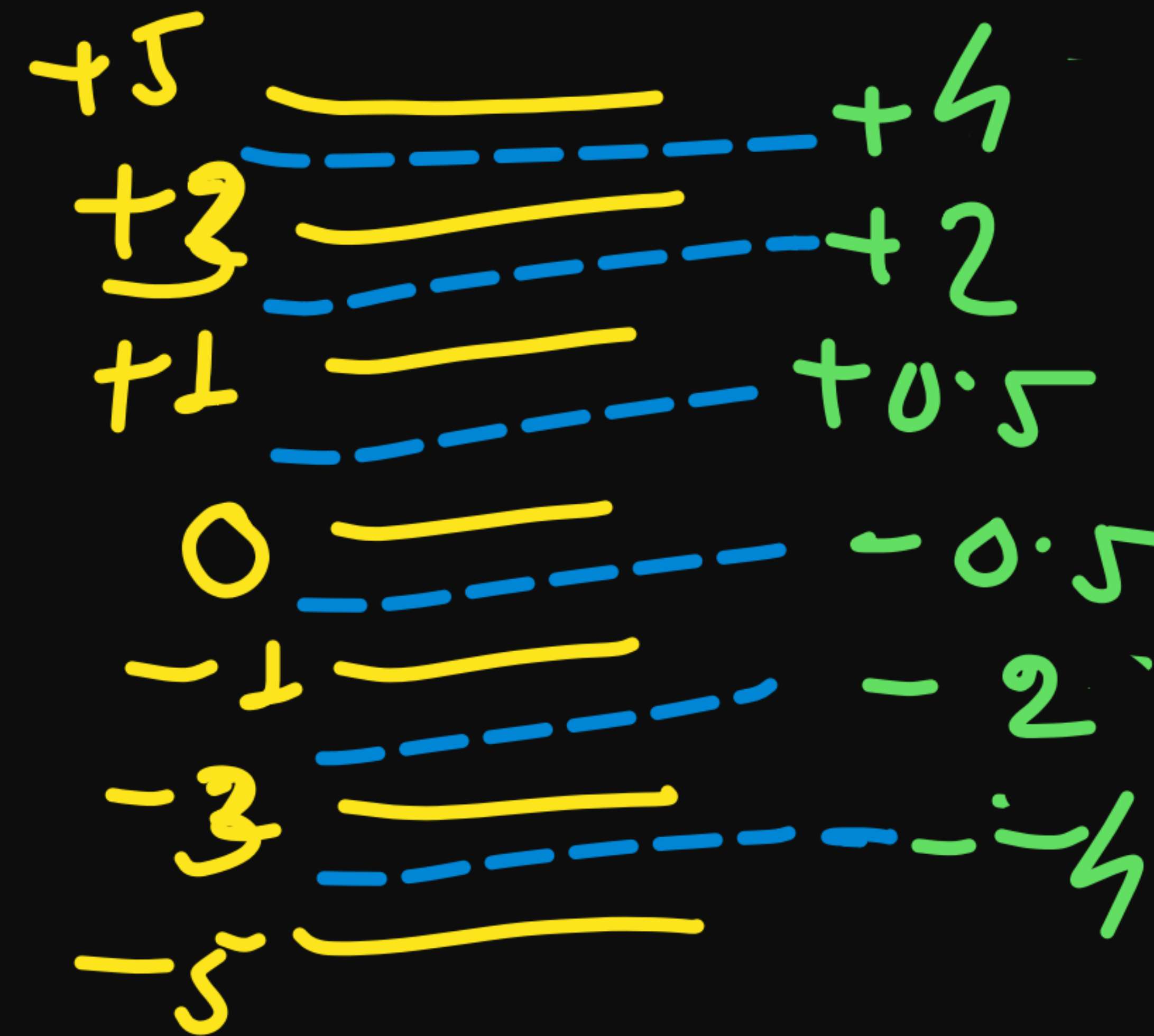
- (A)  $a = 1/6$  and  $b = 1/12$  ✓
- (B)  $a = 1/5$  and  $b = 3/40$  ✗
- (C)  $a = 1/4$  and  $b = 1/16$  ✗
- (D)  $a = 1/3$  and  $b = 1/24$  ✗

[GATE - EC - 2007]

55. Assuming that the reconstruction levels of the quantizer are the mid-points of the decision boundaries, the ratio of signal power to quantization noise power is

- (A)  $\frac{152}{9}$
- (B)  $\frac{64}{3}$
- (C)  $\frac{76}{3}$
- (D) 28

$$\frac{S}{N} = ?$$



Noise Power =  $N$

$$= \left\{ \frac{2^2}{12} \times \frac{1}{6} + \frac{2^2}{12} \times \frac{1}{6} + \frac{1^2}{12} \times \frac{1}{6} \right\} \times 2$$

$$= \frac{2}{12} \left[ \frac{4}{6} + \frac{4}{6} + \frac{1}{6} \right] = \frac{1}{6} \times \frac{9}{6}$$

$$= \frac{3}{12}$$



$$\text{Signal Power} = S = \int_{-5}^5 x^2 f(x) dx = \int_{-5}^{-1} x^2 \frac{1}{12} dx + \int_{-1}^1 x^2 \frac{1}{6} dx + \int_{1}^5 x^2 \frac{1}{12} dx$$

$$S = ?$$

$$\frac{S}{M} = \checkmark$$

$$\int_{-5}^{-1} x^2 \frac{1}{12} dx \neq \int_{-5}^{-3} x^2 \frac{1}{12} dx + \int_{-3}^{-1} x^2 \frac{1}{12} dx$$



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