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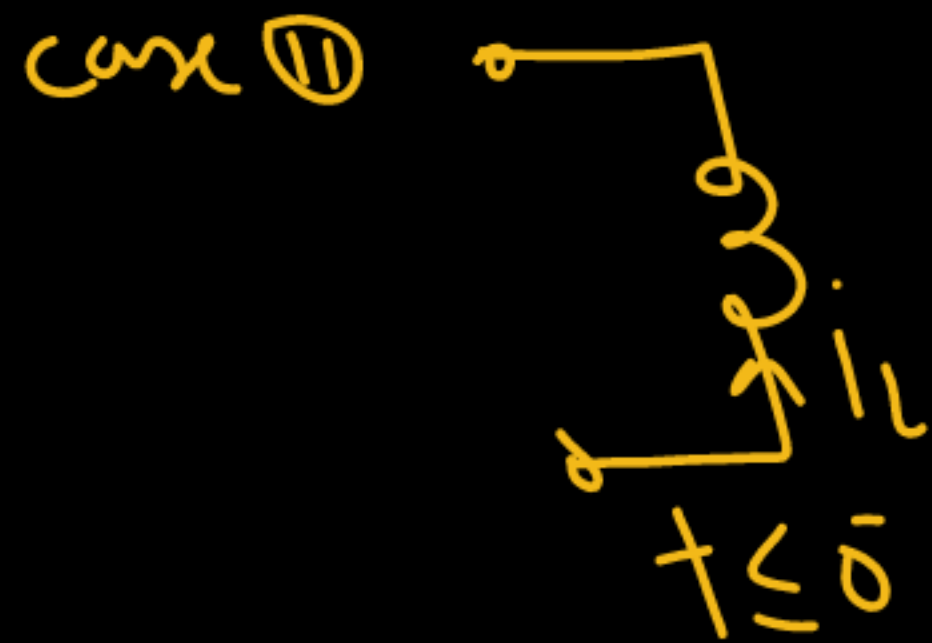
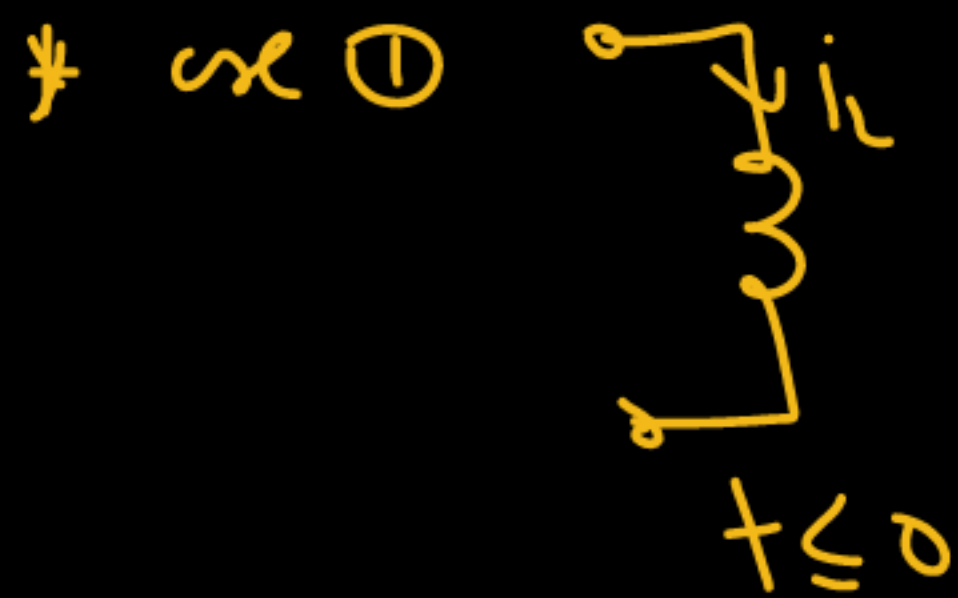
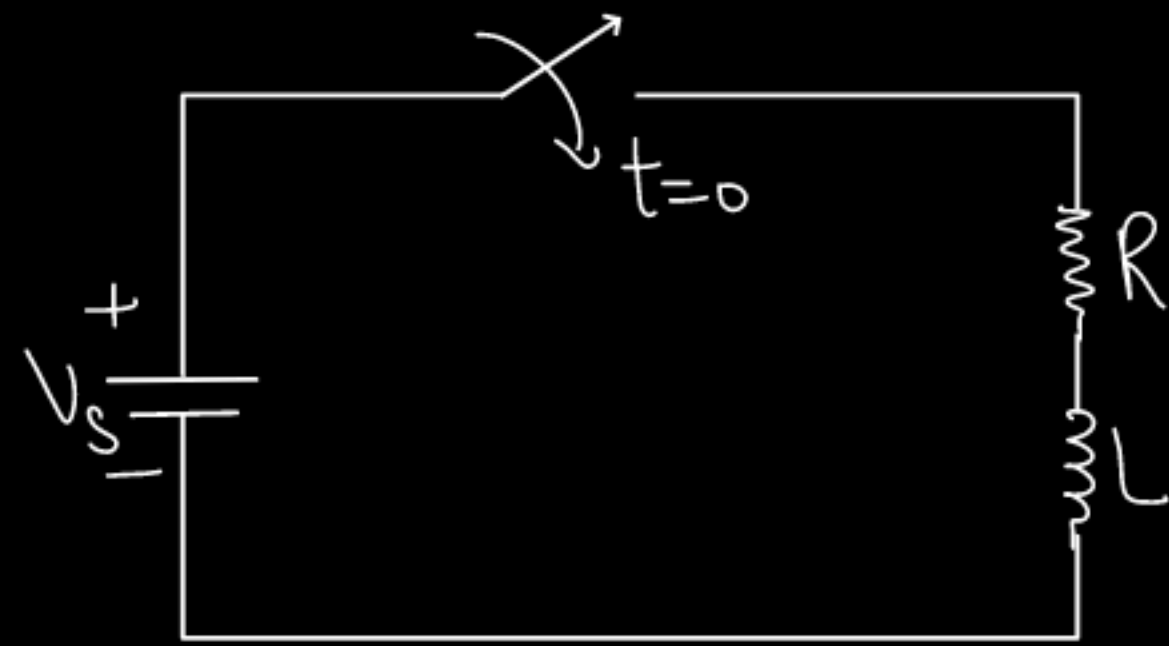
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First order RL Network with initial value and DC excitation

⇒ if inductor is initially charged.
i.e. $i_{L0} \neq 0$ Amp.

* Direction of inductor current must be provided by teacher



let the direction inductor's current for $t \leq 0^-$, is as given in ckt-1.

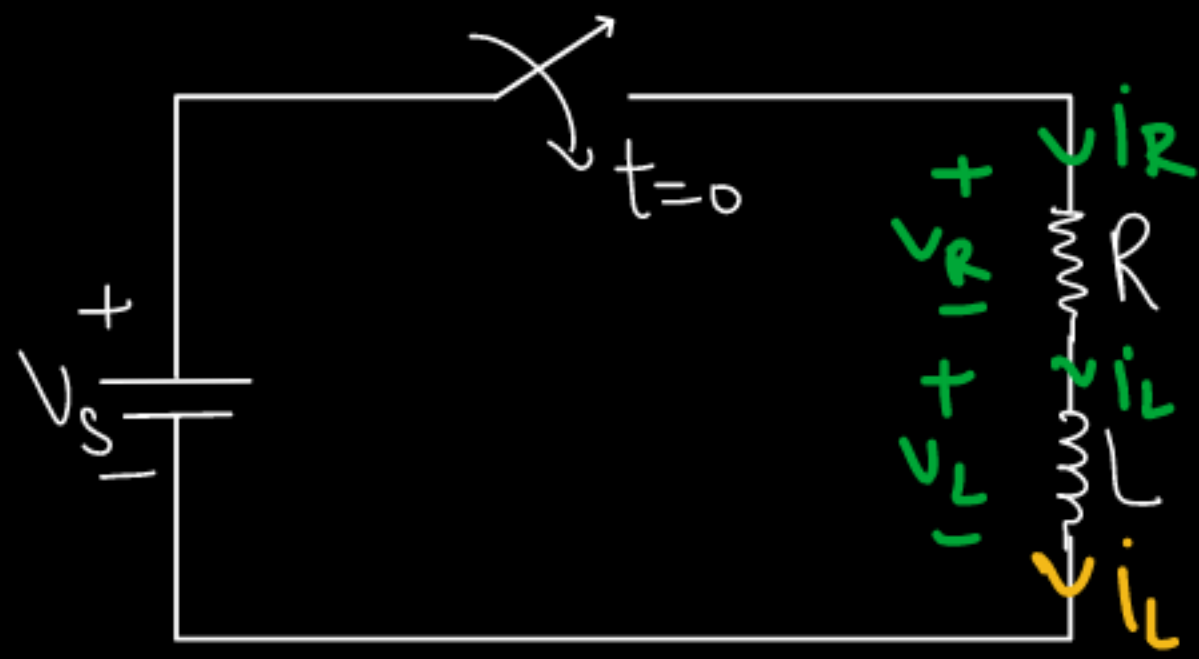
task \Rightarrow

$$i_R(t) = ?$$

$$i_L(t) = ?$$

$$v_L(t) = ? \quad \&$$

$$v_R(t) = ?$$



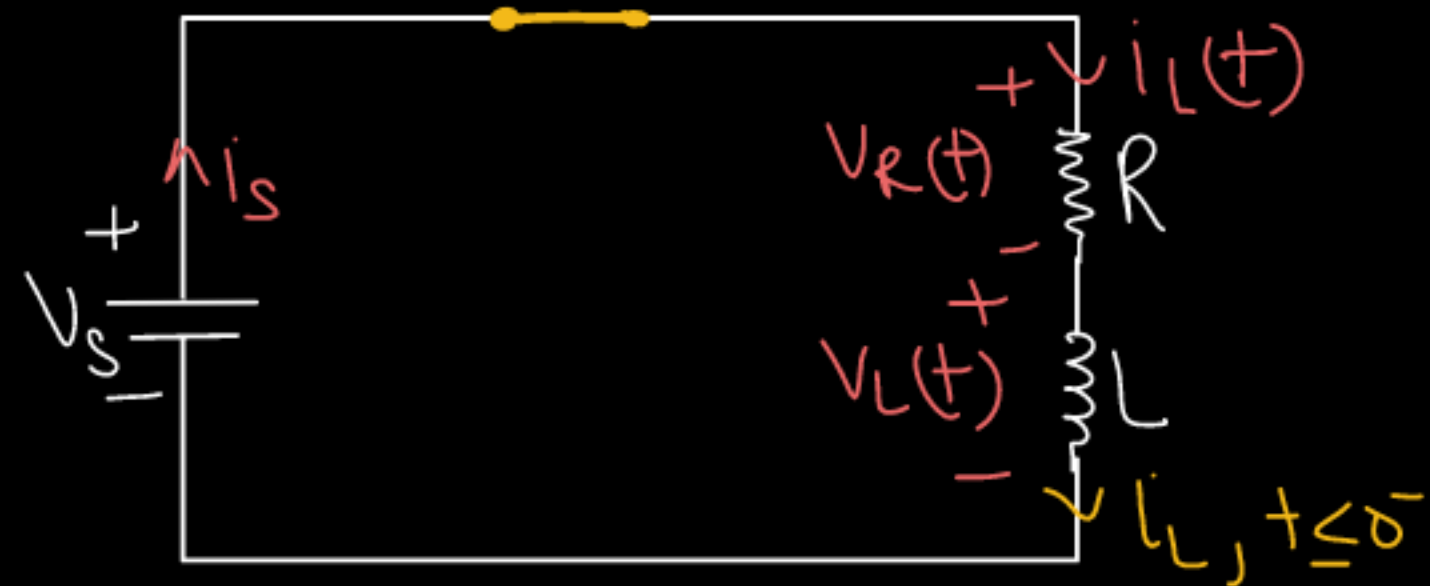
for $t \geq 0$, switch is closed.

$$i_L, t \leq 0^-$$

By KVL \Rightarrow

$$[V_s = v_R(t) + v_L(t)] \quad (1)$$

$$i_R(t) = i_L(t) = i_s(t) \quad (2)$$

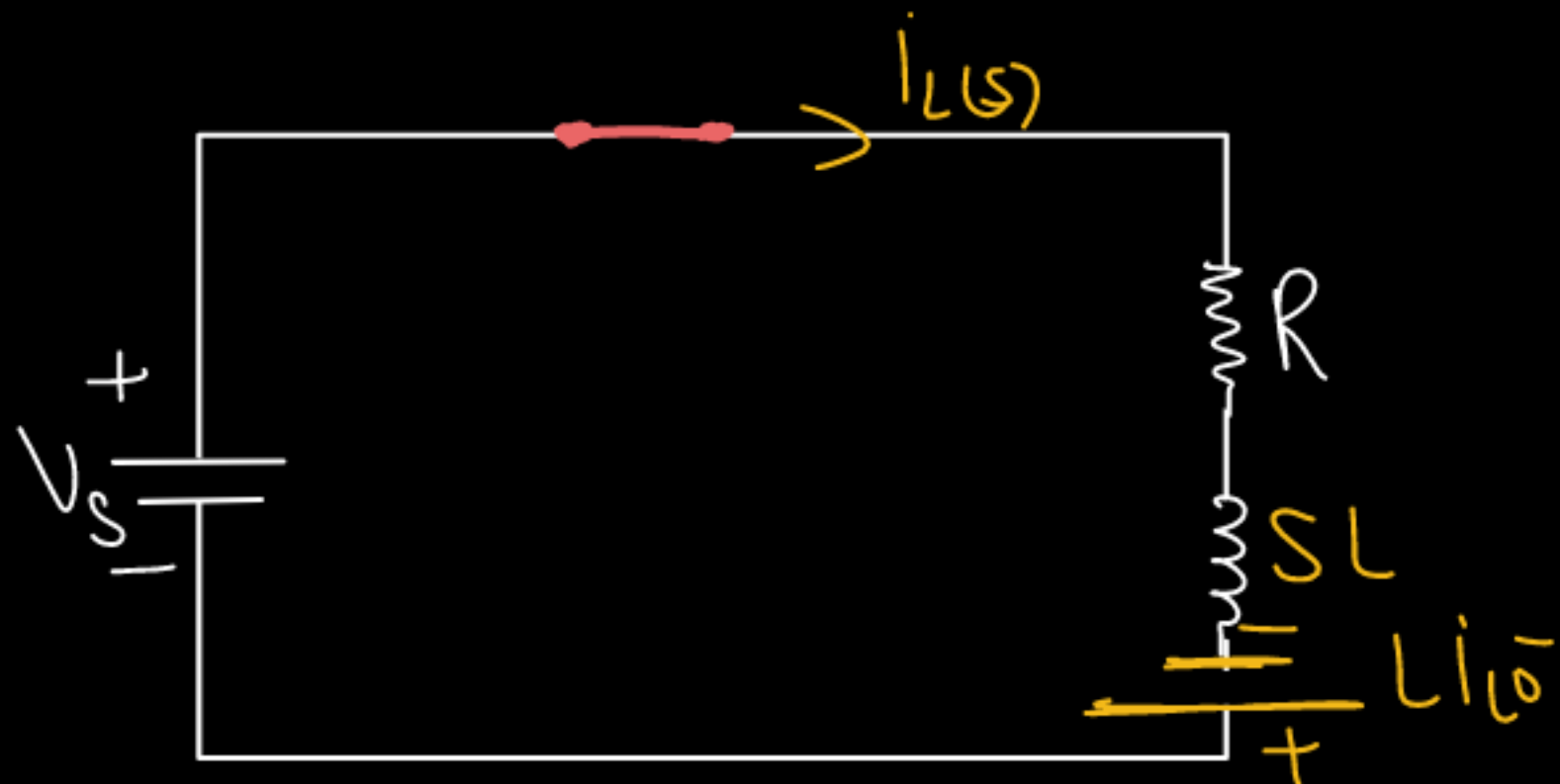


\Rightarrow diffⁿ eqn or lap. transf^m are best mathematical tool to handle this ckt.

- ckt in freq. domain:-

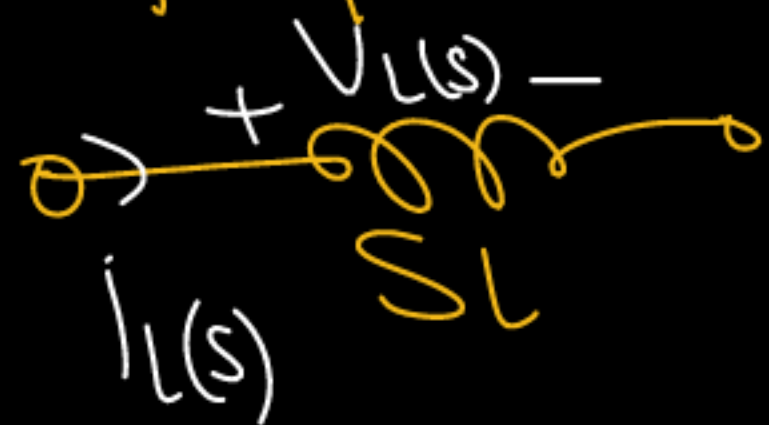
* Supply vol. = $V_s, t \geq 0$

$$L(\text{supply vol.}) = \frac{V_s}{s}$$



*  $i_{L0^-} = 0A$

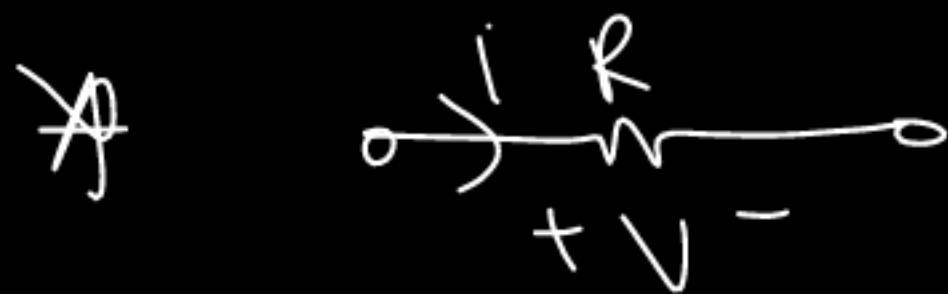
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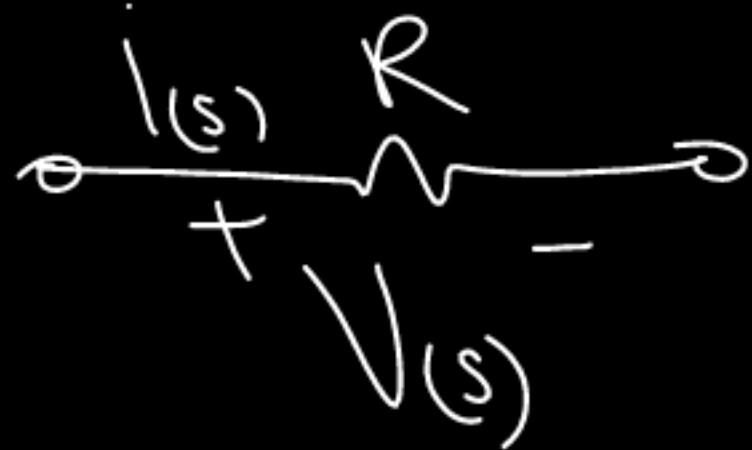
* if inductor's current, $i_{L0^-} \neq 0A$

i.e. $i_{L0^-} = I \text{ Amp.}$

$$\left[V_L(t) = L \frac{di_L(t)}{dt} \right]$$

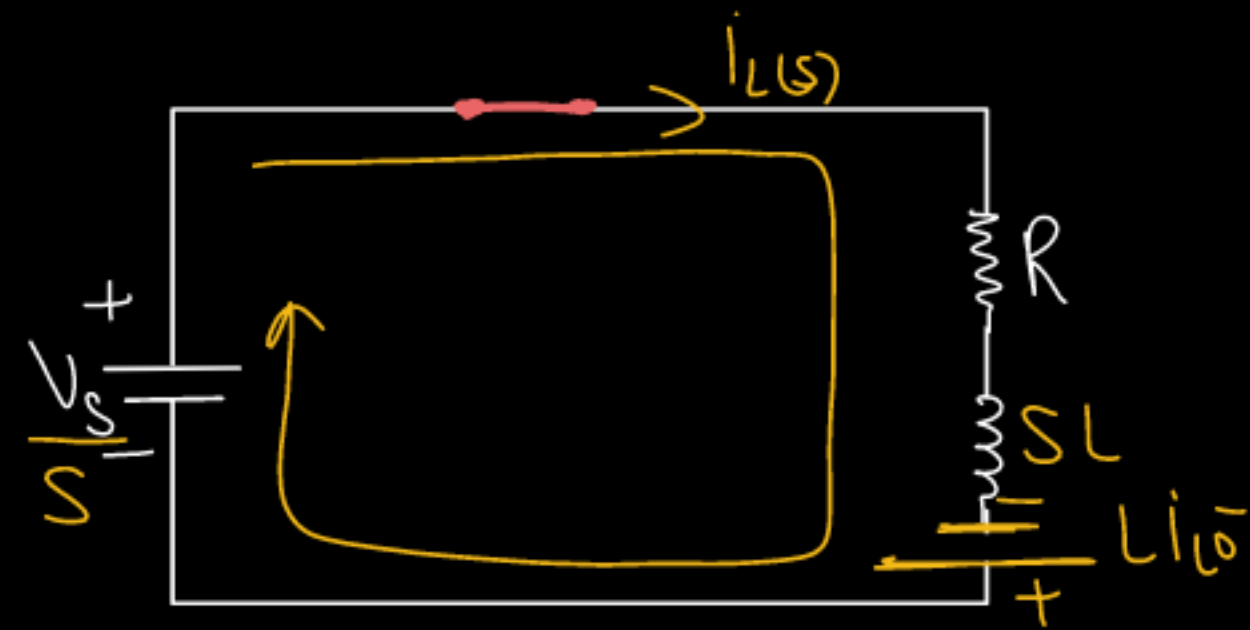


in freq. domain



KVL for given ckt:-

$$\frac{V_s}{s} = i_L(s)(R + sL) - Li_0^-$$



$$i_L(s)(s + R/L)L = \frac{V_s}{s} + Li_0^-$$

$$i_L(s) = \frac{V_s}{L} \left[\frac{1}{s(s + R/L)} \right] + \frac{i_0^-}{(s + R/L)}$$

Break by partial fraction.

$$i_L(s) = \frac{V_s}{R} \left[\frac{1}{s} - \frac{1}{(s + R/L)} \right] + \frac{i_0^-}{(s + R/L)}$$

take invl Lap. trfm.

$$i_L(t) = \frac{V_s}{R} (1 - e^{-R/Lt}) + i_0^- \cdot e^{-R/Lt}, \quad t \geq 0$$

$$[i_L(t) = \frac{V_s}{R}(1 - e^{-R/Lt}) + i_{L0} \cdot e^{-R/Lt}] ; t \geq 0$$

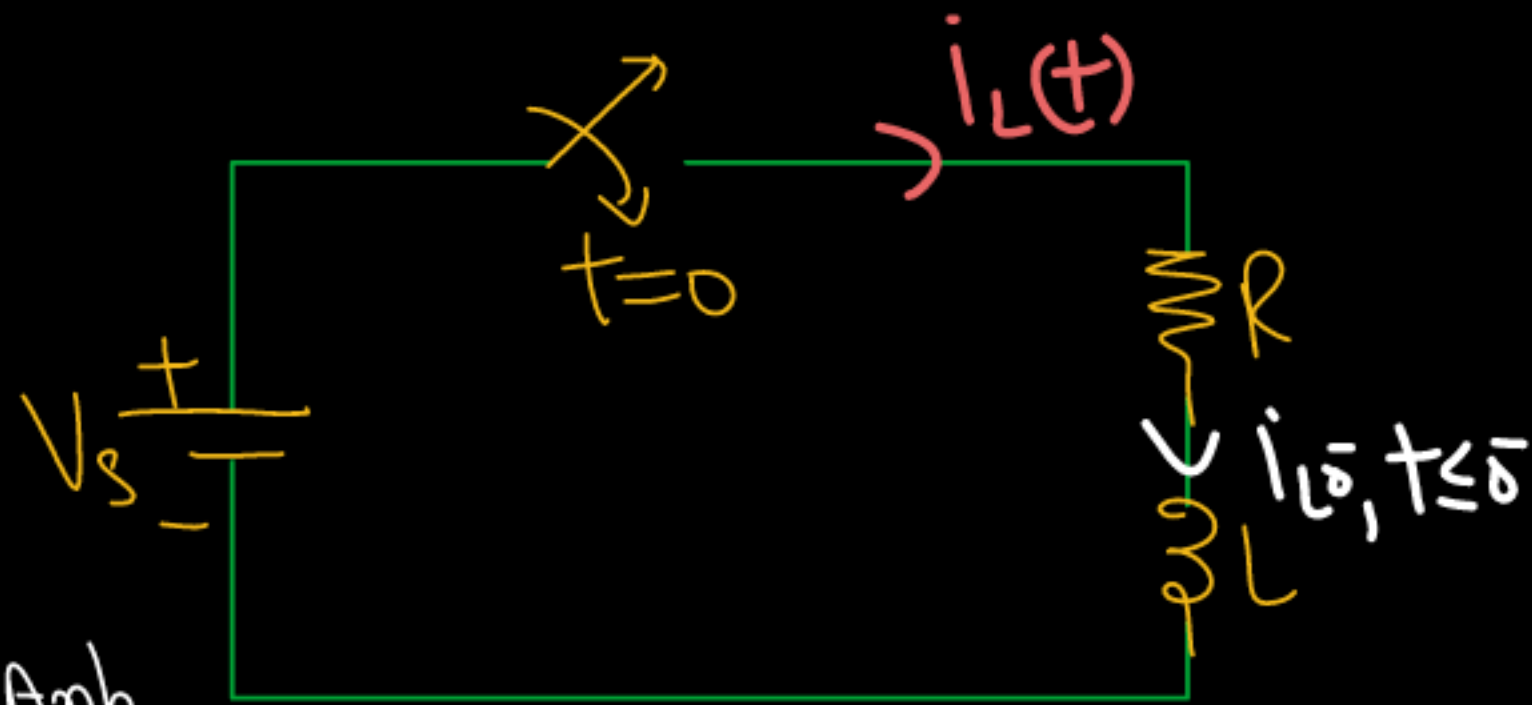
We know that, $\tau = L/R$; for first order RL Network

$$i_L(t) = \frac{V_s}{R}(1 - e^{-t/\tau}) + i_{L0} \cdot e^{-t/\tau}$$

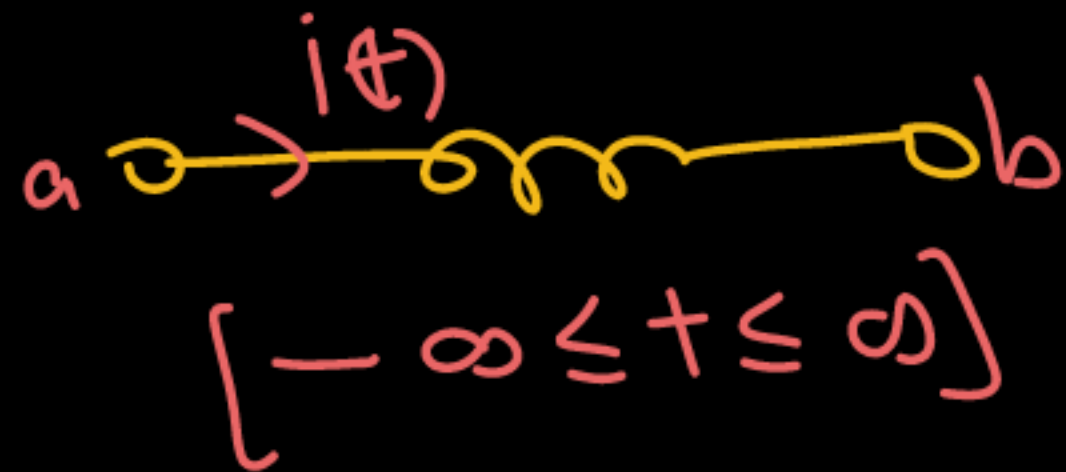
⇒ here

$$i_{L0} = I \text{ Amp}$$

$$i_L(\infty) = i_L(t) \Big|_{t=\infty} = i_L(\infty) = \frac{V_s}{R} \text{ Amp}$$



* current direction of inductor is same for both cases ① $t \leq 0$ ② $t \geq 0$



$$[i_L(t) = \frac{V_s}{R}(1 - e^{-R/Lt}) + i_{L0} \cdot e^{-R/Lt}] ; t \geq 0$$

here $\tau = L/R$, $i_{L0} \Rightarrow$ initial current through inductor

$i_L(\infty) \Rightarrow$ s.s. current of inductor.

$$i_L(\infty) = \frac{V_s}{R} \text{ Amp.}$$

we can modify \rightarrow

$$i_L(t) = i_L(\infty)(1 - e^{-t/\tau}) + i_{L0} e^{-t/\tau}$$

$$i_L(t) = i_L(\infty) - i_L(\infty) \cdot e^{-t/\tau} + i_{L0} \cdot e^{-t/\tau}$$

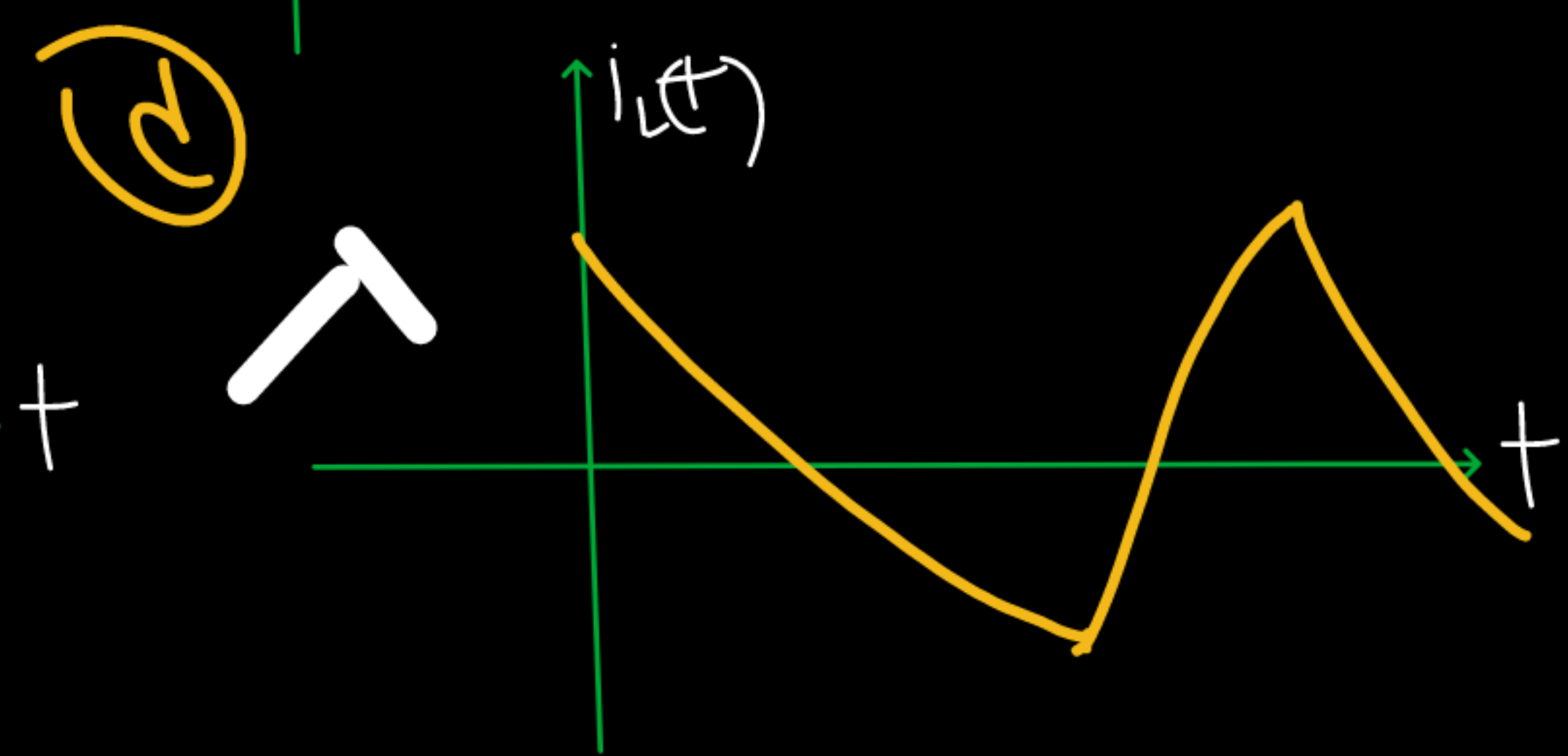
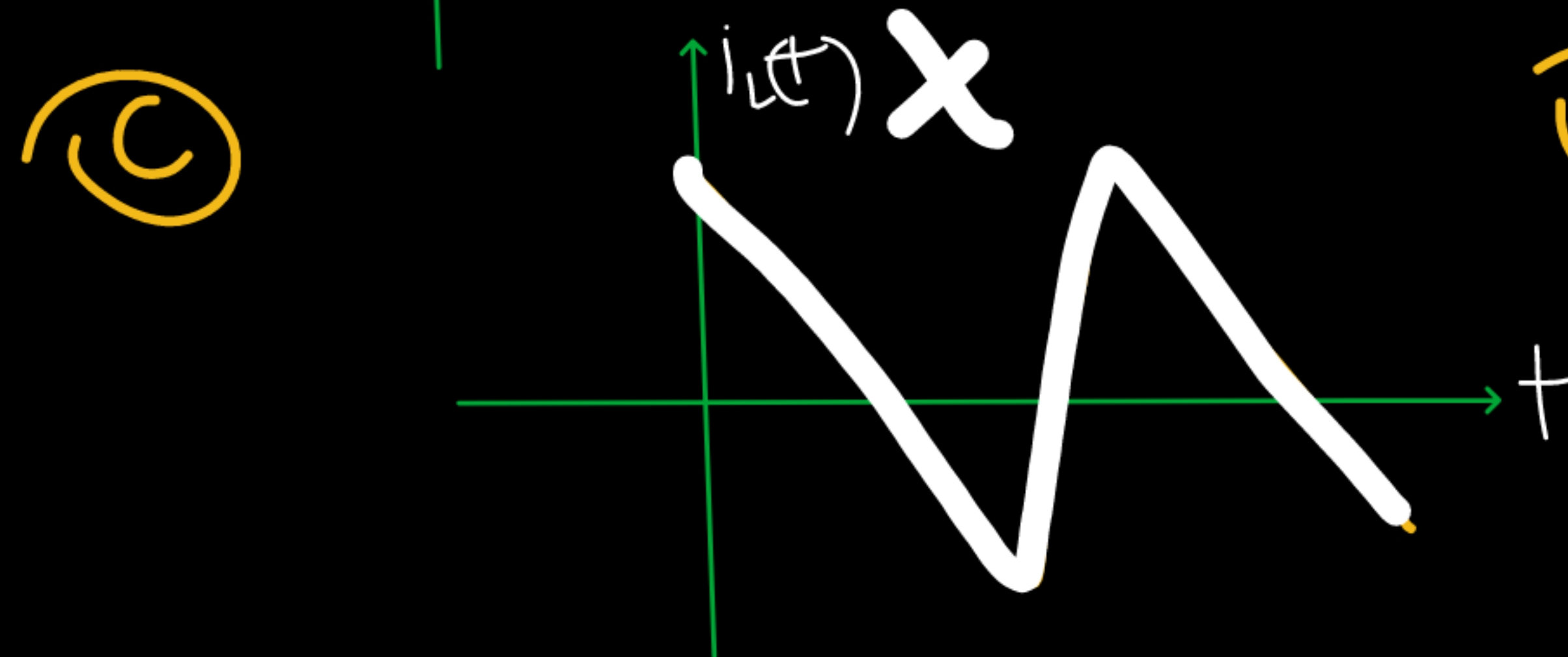
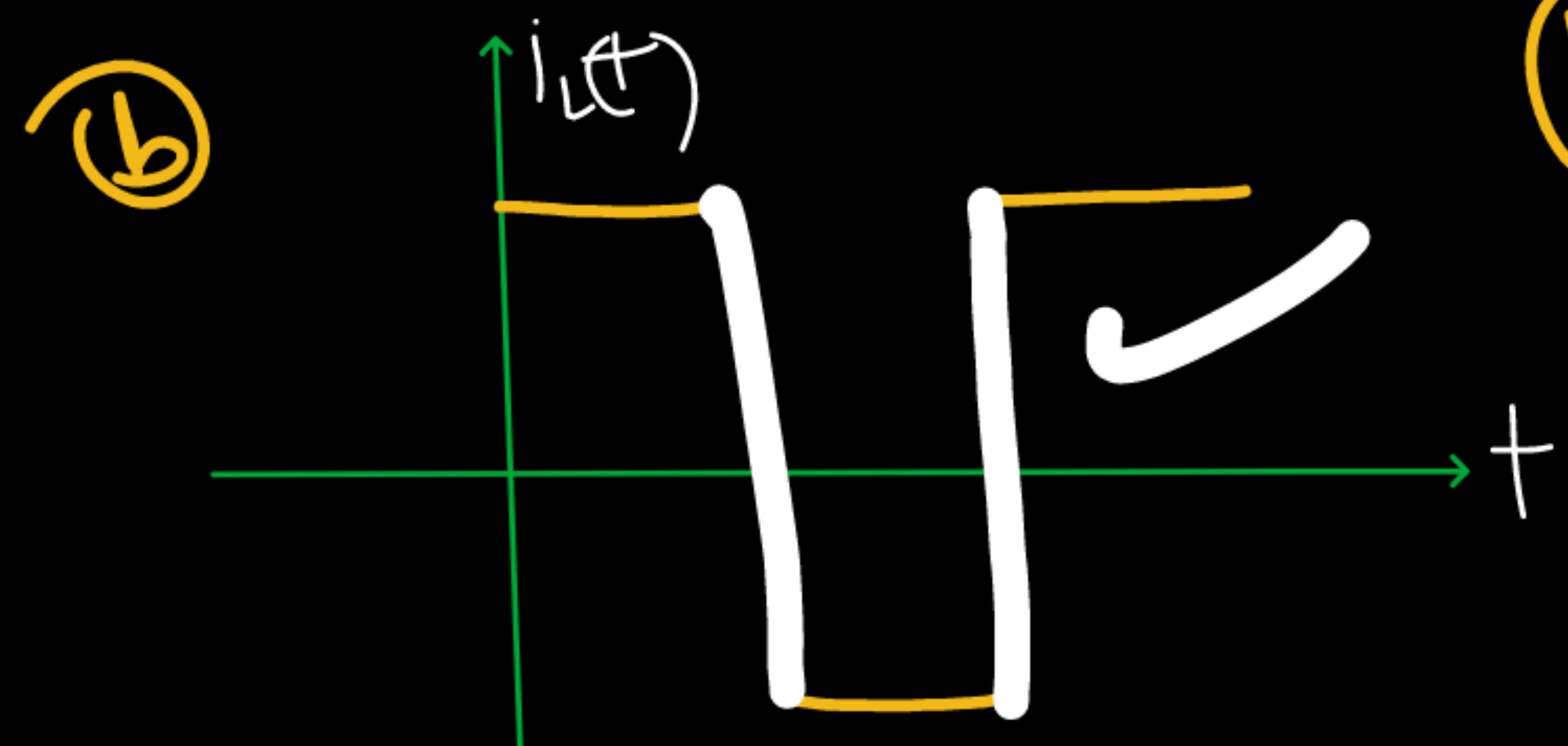
$$i_L(t) = i_L(\infty) + [i_{L0} - i_L(\infty)] e^{-t/\tau} ; t \geq 0$$

V.V. --- ∞ Imp)

\rightarrow
 $\infty \leq$ directions of ind.
 current is same $\leq \infty$

ex in general, which of the following **current** response will not represent inductor's **current** ?

(1.5 marks)



response of Inductor's current :-

