

Test Paper : II	Test Booklet Serial No. :
T . O . I	OMR Sheet No.:
Test Subject : MATHEMATICAL	
SCIENCES	Hall Ticket No.
Test Subject Code: A-15-02	(Figures as per admission card)
Name & Signature of Invigilator	
Name :	Signature:
Paper :	II
•	MATHEMATICAL SCIENCES
Time: 1 Hour 15 Minutes	Maximum Marks : 100
Number of Pages in this Booklet : 8	Number of Questions in this Booklet : 50
Instructions for the Candidates	అభ్యర్థులకు సూచనలు
1. Write your Hall Ticket Number in the space provided on the top	1. ఈ పుట పై భాగంలో ఇవ్వబడిన స్థలంలో మీ హాల్ టికెట్ నంబరు రాయండి.
of this page.	2. ఈ ప్రశ్న పత్రము యాభై బహుళైచ్ఛిక ప్రశ్నలను కలిగి ఉంది.
2. This paper consists of fifty multiple-choice type of questions.	3. పరీక్ష ప్రారంభమున ఈ ప్రశ్నాపత్రము మీకు ఇవ్వబడుతుంది. మొదటి ఐదు
3. At the commencement of examination, the question booklet will be given to you. In the first 5 minutes, you are requested to open	నిమిషములలో ఈ డ్రశ్నాపత్రమును తెరిచి కింద తెలిపిన అంశాలను తప్పనిసరిగా సరిచూసుకోండి.
the booklet and compulsorily examine it as below:	(i) ఈ ప్రశ్న ప్రత్రమును చూడడానికి కవర్పేజి అంచున ఉన్న కాగితపు సీలును
(i) To have access to the Question Booklet, tear off the paper	చించండి. స్టిక్కర్ సీలులేని మరియు ఇదివరకే తెరిచి ఉన్న ప్రశ్నాపత్రమును
seal on the edge of this cover page. Do not accept a booklet	మీరు అంగీకరించవద్దు.
without sticker-seal and do not accept an open booklet.	(ii) కవరు పేజీ పై ముద్రించిన సమాచారం ప్రకారం ఈ ద్రశృపత్రములోని పేజీల
(ii) Tally the number of pages and number of questions in	సంఖ్యను మరియు ప్రశ్నల సంఖ్యను సరిచూసుకోండి. పేజీల సంఖ్యకు
the booklet with the information printed on the cover page. Faulty booklets due to pages/questions missing	సంబంధించి గానీ లేదా సూచించిన సంఖ్యలో డ్రశ్నలు లేకపోవుట లేదా నిజడ్డతి
or duplicate or not in serial order or any other	కాకపోవుల లేదా ప్రశ్నలు క్రమపద్ధతిలో లేకపోవుల లేదా ఏపైనా తేడాలుండుల
discrepancy should be got replaced immediately by a	పంటి దోషపూరితమైన ద్రశ్న ప్రత్నాన్ని వెంటనే మొదటి ఐదు నిమిషాల్లో పరీక్షా
correct booklet from the invigilator within the period	పర్యవేక్షకునికి తిరిగి ఇచ్చివేసి దానికి బదులుగా సరిగ్గా ఉన్న ద్రశ్నపడ్రాన్ని తీసుకోండి. తదనంతరం డ్రశ్నపడ్రము మార్చబడదు ఆదనపు సమయం ఇవ్వబడదు.
of 5 minutes. Afterwards, neither the Question Booklet	(iii) పై విధంగా సరిమానుకొన్న తర్వాత ప్రశ్నావుత్రం సంఖ్యను OMR ప్రత్రము పై
will be replaced nor any extra time will be given.	ఆదేవిధంగా OMR ప్రత్తము సంఖ్యను ఈ ప్రశ్నాప్రత్రము పైనిర్దిష్టర్ట్లుంలో రాయపలెను.
(iii) After this verification is over, the Test Booklet Number should be entered in the OMR Sheet and the OMR Sheet	4. ప్రతి ప్రశ్నకు నాలుగు ప్రత్యామ్నాయ ప్రతిస్పందనలు (A), (B), (C) మరియు (D)
Number should be entered on this Test Booklet.	లుగా ఇవ్వబడ్డాయి. డ్రతిద్రశ్నకు సరైన ద్రతిస్పందనను ఎన్నుకొని కింద తెలిపిన విధంగా
4. Each item has four alternative responses marked (A), (B), (C)	OMR పత్రములో ప్రతి ప్రశ్నా సంఖ్యకు ఇవ్వబడిన నాలుగు వృత్తాల్లో సరైన
and (D). You have to darken the circle as indicated below on the	థ్రతిస్పందనను సూచించే వృత్తాన్ని బాల్ పాయింట్ పెన్తో కింద తెలిపిన విధంగా
correct response against each item.	పూరించాలి.
Example: (A) (B) (D)	
where (C) is the correct response.	(C) సరైన ప్రతిస్పందన అయితే 5. ప్రశ్నలకు ప్రతిస్పందనలను ఈ ప్రశ్నపత్రముతో ఇవ్వబడిన OMR పత్రము పైన
5. Your responses to the items are to be indicated in the OMR Sheet	ఇవ్యబడిన వృత్వాలోనే పూరించి గుర్తించాలి. అలాకాక సమాధాన పత్రంపై పేరొక చోట
given to you. If you mark at any place other than in the circle in	గుర్తిస్తే మీ ప్రతిస్సందన మూల్యాంకనం చేయబడదు.
the Answer Sheet, it will not be evaluated. 6. Read instructions given inside carefully.	6. ప్రశ్న పత్రము లోపల ఇచ్చిన సూచనలను జాగ్రత్తగా చదవండి.
7. Rough Work is to be done in the end of this booklet.	7. చిత్తుపనిని ప్రశ్నపత్రము చివర ఇచ్చిన ఖాళీస్థలములో చేయాలి.
8. If you write your name or put any mark on any part of the OMR	8. OMR పత్రము పై నిర్ణీత స్థలంలో సూచించవలసిన వివరాలు తప్పించి ఇతర స్థలంలో
Answer Sheet, except for the space allotted for the relevant	మీ గుర్తింపును తెలిపే విధంగా మీ పేరు రాయడం గానీ లేదా ఇతర చిహ్నాలను పేట్టడం
entries, which may disclose your identity, you will render yourself	గానీ చేసినట్లయితే మీ అనర్హతకు మీరే బాధ్యులవుతారు.
liable to disqualification. 9. You have to return the test question booklet and OMR Answer	9. పరీక్ష పూర్తయిన తర్వాత మీ ప్రశ్నపత్రాన్ని మరియు OMR పత్రాన్ని తప్పనిసరిగా
Sheet to the invigilators at the end of the examination compulsorily	పరీక్షపర్యవేక్షకుడికి ఇవ్వాలి. వాటిని పరీక్ష గది బయటకు తీసుకువెళ్లకూడదు.
and must not carry it with you outside the Examination Hall.	10. నీరి/నల్ల రంగు బాల్ పాయింట్ పెన్ మాత్రమే ఉపయోగించారి.
10. Use only Blue/Black Ball point pen.	 లాగరిథమ్ బేబుల్స్, క్యాలిక్యులేటర్లు, ఎలక్ష్మానిక్ పరికరాలు మొదలగునవి పరీక్షగదిలో ఉపయోగించడం నిషేదం.
11. Use of any calculator or log table etc., is prohibited.	12 මහා හන අත්ත්ය වන්න වන්න මේ රා

A-15-02







MATHEMATICAL SCIENCES

Paper - II

1. Define $f_n = \frac{x^2}{(1+x^2)^n}$, x is real, n = 0, 1, 2, ...,

then for $x \neq 0$, $\sum_{n=0}^{\infty} f_n(x) =$

- (A) 0
- (C) 1 + x
- **2.** The function $f(x) = \sin(1/x)$, x > 0 is
 - (A) Uniformly continuous on R⁺
 - (B) Uniformly continuous on R
 - (C) Continuous on R⁺
 - (D) Not continuous on R⁺
- **3.** $\int_0^1 x (1-x^2)^n dx =$

- (A) 1 (B) $\frac{1}{2}$ (C) $\frac{1}{2(n+1)}$ (D) $\frac{1}{(2n+1)}$
- **4.** If p > 0 and $\alpha \in \mathbb{R}$, then $\lim_{n\to\infty} \frac{n^{\alpha}}{(1+n)^n} =$
 - (A) 0
- (B) 1
- (C) ∞
- (D) not defined
- 5. If T: $R^3 \rightarrow R^2$ is a linear transformation defined by T (x, y, z) = (x + 2y - z, y + z,x + y - 2z), then the rank of T is equal to
 - (A) 0
- (B) 1
- (C) 2
- (D) 3
- 6. Let A and B be nxn matrices with real numbers as elements. Then which one of the following statements is NOT true?
 - (A) Rank of A = Rank of A'
 - (B) Rank of (AB) = Rank of (BA)
 - (C) Rank of (A + B) < Rank of A + Rank of B
 - (D) If C is obtained after a finite number of elementary operations on A, then Rank of A = Rank of C

7. The largest eigen value of the matrix

 $A = \begin{bmatrix} 3 & 10 & 5 \\ -2 & -3 & -4 \\ 3 & 5 & 7 \end{bmatrix}$ is

- (A) 2
- (B) 3
- (C) 4
- (D) 6
- **8.** Let T: $R^3 \rightarrow R$ be a linear transformation defined by T (1,1,1) = 3, T (0,1,-2) = 1and T (0, 0, 1) = -2

Then T(x, y, z) =

- (A) 8x + 3y 2z (B) 3x 8y 2z
- (C) 8x 3y 2z (D) 2x 3y + 8z
- **9.** If f(z) = u(x, y) + iv(x, y) and g(z) = u(x, y) - iv(x, y) are analytic functions defined on the same domain and f(1 + i) = 2 + 3i, then g(4 + 3i) =
 - (A) 4 + 3i
- (B) 4 3i
- (C) 2 + 3i
- (D) 2 3i
- 10. If an entire function f (z) is bounded in absolute value for all z, then f (z) =
 - (A) Constant
- (B) e^z
- (C) 1/z
- (D) z
- **11.** If f (z) = sinz + e^{3z} , then $\frac{\partial f(z)}{\partial \overline{z}}$ =
 - (A) 0
- (B) 3e^{3z̄}
- (C) cos \overline{z}
- (D) $\cos \overline{z} + 3e^{3\overline{z}}$
- **12.** The residue of f (z) = $\frac{z^2 + 3z + 2}{z^2(z-1)}$ at z = 0 is
 - (A) 0
- (B) -1 (C) 2
- (D) 5



- 13. If G is a finite abelian group, then G is isomorphic to the direct product of its
 - (A) normal subgroups
 - (B) abelian subgroups
 - (C) sylow subgroups
 - (D) cyclic subgroups
- **14.** Which one of the following is NOT true?
 - (A) There are $\phi(n)$ premature n-th roots of unity where $\phi(n)$ is the Euler φ - function
 - (B) If ωis a primitive n-th root of unity, then $F_0(\omega)$ is the splitting field of $x^n - 1$ over F
 - (C) If $\omega_1, \omega_2, ..., \omega_{\phi(n)}$ are the primitive n-th roots of unity, then any automorphism of $F_0(\omega_1)$ takes ω_1 into some ω
 - (D) $[F_0(\omega_1):F_0] > \phi(n)$
- 15. If R is a commutative ring with unit element and M is an ideal of R, then M is a maximal ideal of R if and only if R/M is
 - (A) a quotient ring (B) a field
 - (C) a division ring (D) an ideal
- **16.** The solution of $x^2 \oplus 1 = 0$ in the field (Z_5, \oplus, \bullet) is
 - (A) 0, 1 (B) 1, 2 (C) 2, 3 (D) 3, 4
- 17. The number of units in the domain of Gaussian integers is
 - (A) 1
- (B) 2
- (C) 3
- (D) 4

- **18.** Consider the linear space X = C[0, 1]with norm $||f|| = \sup\{|f(t)| : 0 \le t \le 1\}$. Let $F = \{f \in X : f(\frac{1}{2}) = 0\}$ and $G = \{g \in X : g(\frac{1}{2}) \neq 0\}$. Then
 - (A) F is not closed and G is open
 - (B) F is closed but G is not open
 - (C) F is not closed and G is not open
 - (D) F is closed and G is open
- 19. An integrating factor for the differential equation $ydx + (x^2y - x) dy = 0$ is
- (B) 1/x (C) $1/x^2$ (D) e^x
- **20.** For the differential equation $y''-x^2y'-xy=0$ an equivalent system of first order equations is
 - (A) dv/dx = v+z; $dz/dx = x^2z + v$
 - (B) dv/dx = z: $dz/dx = xv + x^2z$
 - (C) dy/dx = xz; dz/dx = y + xz
 - (D) dy/dx = x + z; $dz/dx = y + x^2z$
- 21. The eigen functions of the Sturm Liouville problem $x'' + \alpha x = 0$, x(0) = 0 and x(1) = 0, for $0 \le t \le 1$, n = 0, 1, 2, ... are
 - (A) $x_n(t) = \sin(2n+1)\pi t$
 - (B) $x_n(t) = \cos(2n+1) \pi t/2$
 - (C) $x_n(t) = \sin(2n+3) \pi t/2$
 - (D) $x_n(t) = \cos(2n+3) \pi t/2$
- **22.** The stationary function of $\int_{0}^{4} (xy' y'^2) dx$ subject to y(0) = 0 and y(4) = 3 is
 - (A) $v = \frac{1}{2}(x^2 1)$ (B) $v = \frac{1}{2}(x^2 + 1)$
 - (C) $y = \frac{1}{4}(2x^2 + x)$ (D) $y = \frac{1}{4}(x^2 x)$

23. The general form of Hamiltonian equations of motion for a conservative holonomic dynamical system for k = 1, 2, 3, ..., n are

(A)
$$\dot{q}_k = \frac{\partial H}{\partial t_k}, \, \dot{p}_k = -\frac{\partial H}{\partial q_k}$$

(B)
$$\dot{q}_k = -\frac{\partial H}{\partial t_k}, \, \dot{p}_k = -\frac{\partial H}{\partial q_k}$$

(C)
$$q_k = \frac{\partial H}{\partial t_k}, p_k = -\frac{\partial H}{\partial t_k}$$

(D)
$$q_k = \frac{\partial H}{\partial t_k}, p_k = -\frac{\partial H}{\partial p_k}$$

- **24.** If the kinetic energy of a body of mass m moving in one-dimension is $\frac{1}{2} mx^{2}$ and its potential energy is $\frac{1}{2} kx^{2}$ where k is a constant then its Lagrange's equations of motion is
 - (A) $k\ddot{x} + mx = 0$
- (B) $m\ddot{x} + kx = 0$
- (C) $m\dot{x} + kx = 0$
- (D) $k\ddot{x} + m\dot{x} = 0$
- **25.** The resolvent kernel $R(x,t;\lambda)$ for the $K(x,t) = x^2t^2$, a = -1, b = 1 is

(A)
$$\frac{3x^2t^2}{1-2\lambda}$$
, $|\lambda| < \frac{1}{2}$ (B) $\frac{4x^2t^2}{3-2\lambda}$, $|\lambda| < 3/2$

(C)
$$\frac{5x^2t^2}{5-2\lambda}$$
, $|\lambda| < 5/2$ (D) $\frac{5x^2t^2}{5+2\lambda}$, $|\lambda| < 2/5$

26. The solution of the partial differential equation (y - z)p + (z - x)q = x - y is

(A)
$$f(x + y + z) = x^2 + y^2 + z^2$$

(B)
$$f(x + y + z) = xy + yz + zx$$

(C)
$$f(x^2 + y^2 + z^2) = xyz$$

(D)
$$f(x^2 + y^2 + z^2) = x + y + z$$

27. The solution of the partial differential equation $3 \frac{\partial u}{\partial x} + 2 \frac{\partial u}{\partial y} = 0$, $u(x,0) = 4e^{-x}$

(A)
$$2e^{5x+3y}+2e^{-3x+2y}$$

(B)
$$3e^{-5x+3y}+e^{3x-2y}$$

(C)
$$4e^{-(2x-3y)/2}$$

(D)
$$4e^{-(3x-2y)/2}$$

- **28.** The Newton-Raphson method of finding a root of a polynomial or transcendental equation has the rate of convergence
 - (A) 3
- (B) 2
- (C) 1.67
- (D) 1.4
- **29.** An approximate solution for the system of linear equations

$$10x + 2y + z = 9$$
, $2x + 20y - 2z = -44$;
-2x + 3y + 10z = 22 using Gauss-Seidal method is

(A)
$$x = 1.094$$
, $y = -1.908$, $z = 2.946$

(B)
$$x = 1.082$$
, $y = -1.914$, $z = 2.965$

(C)
$$x = 1.108$$
, $y = -1.932$, $z = 2.981$

(D)
$$x = 1.013$$
, $y = -1.996$, $z = 3.001$

- **30.** The value of the integral $I = \int_0^6 \frac{dx}{1+x^2}$ by using Simpson's 1/3 rule, is
 - (A) 1.2886
- (B) 1.3268
- (C) 1.3662
- (D) 1.3874
- 31. For any discrete distribution
 - (A) $S.D \ge M.D$ from mean
 - (B) S.D = M.D
 - (C) S.D < M.D from mean
 - (D) No relation between S.D and M.D



- **32.** For a random variable x moments of all order exit and μ_i denote j^{th} central moment, then
 - (A) $\mu_{2j+1}^2 > \mu_{2i} \mu_{2i+2}$
 - (B) $\mu_{2i+1}^2 < \mu_{2i} \mu_{2i+2}$
 - (C) $\mu_{2i+1} = \mu_{2i} \mu_{2i+2}$
 - (D) either B or C is correct
- **33.** The probability distribution of a random variable X is $f(x) = k \sin(\pi x/5)$, $0 \le x \le 5$, then the ratio between median of X and k is
 - (A) $25:\pi$
- (B) 5:2
- (C) 1:2
- (D) $10:\pi$
- **34.** If ϕ (t) denotes the characteristic function of a random variable, then
 - i) $\phi(0) = 1$,
 - ii) $\phi(t) \leq 1$,
 - iii) φ(t) is continuous every where
 - (A) only i) is correct but not ii) and iii)
 - (B) only ii) is correct but not iii)
 - (C) all i), ii) and iii) are correct
 - (D) none of i), ii) and iii) are correct
- **35.** If you wish to estimate the proportion of engineers and scientists who have studied statistics and you wish your estimate to be correct within 2% with probability 0.95 or more, how large sample would you take if you have no idea what the true proportion is?
 - (A) 1200
- (B) 800
- (C) any number
- (D) 95

- 36. The Poisson process satisfies the following conditions
 - (A) regularity
 - (B) homogeneity
 - (C) independent increments
 - (D) all the above three (A), (B) and (C)
- **37.** For a Binomial distribution with p = 0.5 has maximum probability when
 - (A) X = n/2 if n is even
 - (B) $x = \frac{1}{2}(n-1)$ and $x = \frac{1}{2}(n+1)$ if n is odd
 - (C) x = n
 - (D) both A) and B) are correct
- **38.** The probability mass function of a Poisson variate with parameter λ truncated at 0 is

(A)
$$\frac{e^{-\lambda}\lambda^x}{x!}$$
 (B) $\frac{e^{-\lambda}\lambda^x}{x!}(1-e^{-\lambda})$ (C) $\frac{e^{-\lambda}\lambda^x}{x!(1-e^{-\lambda})}$ (D) $1-e^{-\lambda}$

(B)
$$\frac{e^{-\lambda}\lambda^x}{x!} \left(1 - e^{-\lambda}\right)$$

(C)
$$\frac{e^{-\lambda}\lambda^x}{x!(1-e^{-\lambda})}$$

(D)
$$1 - e^{-\lambda}$$

- **39.** Let x_1, x_2, \dots, x_n be a random sample drawn from an exponential distribution with parameter λ , then the distribution function of Y = min($x_1, x_2, ..., x_n$) is
 - (A) $n(n-1)(1-e^{-n\lambda y})$
 - (B) $\left(1-e^{-n\lambda y}\right)$
 - (C) $\frac{1}{2} n(n-1) (1-e^{-n\lambda y})$
 - (D) $\left(1-e^{-\lambda y}\right)$

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- 40. The minimum variance bound estimator for θ in a Cauchy population with parameter θ is
 - (A) sample mean
 - (B) sample median
 - (C) reciprocal of sample median
 - (D) does not exist
- 41. In a Poisson distribution with unit mean the mean deviation about mean is
 - (A) 2/e
- (B) e/2 (C) e
- (D) 1
- 42. With normal notations the variance of M.L.E. is
 - (A) $I(\theta)$
- (B) $1/I(\theta)$
- (C) $\sqrt{I(\theta)}$ (D) $-1/I(\theta)$
- 43. Neyman-Pearson lemma provides
 - (A) An unbiased test
 - (B) a most powerful test
 - (C) an admissible test
 - (D) sufficient test
- **44.** With the usual notation the sum of squares due to any factorial effect is
 - (A) $\frac{()^2}{\sum \gamma_i c_i^2}$ (B) $\frac{()^2}{\sum \gamma_i^2 c_i}$

 - (C) $\frac{()^2}{\sum \gamma_i^2}$ (D) $\frac{()^2}{\sum \gamma_i c_i}$
- 45. The information on auxiliary variate is used in the following sampling scheme
 - (A) double sampling
 - (B) two stage sampling
 - (C) cluster sampling
 - (D) quota sampling

- 46. The arrival rate and service rates of a M/M/1 queueing system are 3 and 4, then the probability of system emptiness is
 - (A) 0.25
- (B) 0.75
- (C) 0.3
- (D) 0.5
- 47. A simplex is a
 - (A) half plane
 - (B) convex polyhedran
 - (C) hull
 - (D) envelop
- **48.** If $A = [a_{ii}]$ is the payoff matrix then saddle point exist when
 - (A) $Min_j Max_i a_{ij} = Max. Min a_{ij}$
 - (B) $Min_i Max_i a_{ii} < Max. Min a_{ii}$
 - (C) Min_{i} Max_{i} a_{ii} > Max. $Min a_{ij}$
 - (D) All the above three are correct
- **49.** If f(x) is the p.d.f of a life time distribution then the hazard rate of distribution is
 - (A) f(x)/F(x)
 - (B) f(x)/(1-F(x))
 - (C) F(x)/f(x)
 - (D) $\log f(x)/(1 F(x))$
- 50. The variance covariance matrix of a

random vector $\overline{\mathbf{x}}$ is $\Sigma = \begin{bmatrix} 4 & 0 & 0 \\ 0 & 8 & 2 \\ 0 & 2 & 8 \end{bmatrix}$, then

the first principal component explains _____ percentage of variations on the dependent variable.

- (A) 90
- (B) 45
- (C) 50

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(D) 60



Space for Rough Work

