

29/01/2025 Evening



Memory Based Answers & Solutions

Time : 3 hrs. M.M. : 300

JEE (Main)-2025 (Online) Phase-1

(Physics, Chemistry and Mathematics)

IMPORTANT INSTRUCTIONS:

- (1) The test is of 3 hours duration.
- (2) This test paper consists of 75 questions. Each subject (PCM) has 25 questions. The maximum marks are 300.
- (3) This question paper contains **Three Parts**. **Part-A** is Physics, **Part-B** is Chemistry and **Part-C** is **Mathematics**. Each part has only two sections: **Section-A** and **Section-B**.
- (4) Section A: Attempt all questions.
- (5) Section B: Attempt all questions.
- (6) Section A (01 20) contains 20 multiple choice questions which have only one correct answer. Each question carries +4 marks for correct answer and –1 mark for wrong answer.
- (7) Section B (21 25) contains 5 Numerical value based questions. The answer to each question should be rounded off to the nearest integer. Each question carries +4 marks for correct answer and -1 mark for wrong answer.



PHYSICS

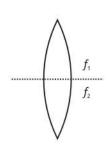
SECTION - A

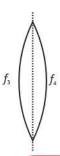
Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

 An equiconvex lens is cut in two ways as shown. If the focal lengths of the parts are as mentioned in the diagram. Find

 $\frac{f_1}{f_3}$





(1) 2

(2) 4

(3) $\frac{1}{2}$

(4) $\frac{1}{4}$

Answer (3)

Sol. $f_1 = f_2 = f$

$$f_3 = f_4 = 2f$$

$$\frac{f_1}{f_2} = \frac{1}{2}$$

2. Three identical particles, each of mass *m* move under the influence of mutual attractive forces. Initially the are on the vertices of an equilateral triangle of side 'a' and have equal speed *v* directed towards the adjacent particle as shown. The net angular momentum about the centre just before collision is



- $(1) \quad \frac{3mva}{2}$
- (2) $\frac{2}{3}mvc$
- (3) $\frac{\sqrt{3}}{2}mva$
- (4) $\frac{2}{\sqrt{3}}$ mvc

Answer (3)

Sol. Net angular momentum remains conserved as there is zero net torque about centroid.

$$\Rightarrow L_i = L_f$$

$$L_f = \frac{3amv}{2\sqrt{3}} = \frac{\sqrt{3}}{2}mva$$

- 3. A solenoid of radius 10 cm carrying current 0.29 A and having total 200 turns. If magnetic field inside solenoid is 2.9×10^{-4} T. Find length of solenoid.
 - (1) 6π cm
- (2) $8 \pi \text{ cm}$
- (3) $4.5 \pi \text{ cm}$
- (4) 16 π cm

Answer (2)

Sol. $B = \mu_0 n_i$

$$2.9 \times 10^{-4} = 4\pi \times 10^{-7} \times \frac{200}{4} \times 0.29$$

 $L = 8 \pi \text{ cm}$

Column-I

 Match the physical quantities with their corresponding dimensions

	Columnia		Columni-ii
(A)	Young's modulus	(i)	[AL ²]
(B)	Magnetic moment	(ii)	$[ML^2T^{-2}A^{-1}]$
(C)	Magnetic flux	(iii)	[AL ⁻¹]
(D)	Magnetic intensity	(iv)	$[ML^{-1}T^{-2}]$

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- (1) $A \rightarrow (iv)$, $B \rightarrow (i)$, $C \rightarrow (ii)$, $D \rightarrow (iii)$
- (2) $A \rightarrow (iv), B \rightarrow (ii), C \rightarrow (i), D \rightarrow (iii)$
- (3) $A \rightarrow (iii), B \rightarrow (i), C \rightarrow (ii), D \rightarrow (iv)$
- (4) $A \rightarrow (iii), B \rightarrow (ii), C \rightarrow (i), D \rightarrow (iv)$

Answer (1)

Sol. Young's modulus
$$\equiv \frac{F}{A} \equiv \left[ML^{-1}T^{-2} \right]$$

Magnetic moment
$$\equiv IA \equiv \left[AL^2 \right]$$

Magnetic flux
$$\equiv Vt \equiv \left[ML^2T^{-2}A^{-1} \right]$$

Magnetic intensity
$$\equiv H = nI \equiv \left\lceil AL^{-1} \right\rceil$$

- 5. Two particles of same mass are performing SHM vertically with two different springs of spring constants K_1 and K_2 . If amplitude of both is same. Find ratio of the maximum speed of two particles.
 - $(1) \quad \sqrt{\frac{K_1}{K_2}}$
- $(2) \sqrt{K_2 K_1}$
- (3) $\sqrt{\frac{K_2}{K_1}}$
- (4) $\sqrt{\frac{K_1 + K_2}{K_1 K_2}}$

Answer (1)

Sol.
$$V_{\text{max}} = A\omega$$

$$\frac{V_1}{V_2} = \frac{\omega_1}{\omega_2} = \sqrt{\frac{K_1}{K_2}}$$

- 6. A physical quantity Q is given as $Q = \frac{ab^4}{cd}$, if the percentage error is a, b, c and d are 2%, 1%, 2% and 1%,
 - the % error in Q will be
 - (1) 5%

(2) 15%

(3) 9%

(4) 2%

Answer (3)

Sol.
$$\frac{\Delta Q}{Q} = \frac{\Delta a}{a} + \frac{4\Delta b}{b} + \frac{\Delta c}{c} + \frac{\Delta d}{d}$$
$$= 2\% + 4\% + 2\% + 1\%$$
$$= 9\%$$

7. **Assertion**: On increasing the pressure, the volume decrease is more in an isothermal process than in an adiabatic process.

Reason: Adiabatic process is given by PV'.

- (1) Assertion is correct and Reason is false
- (2) Assertion is correct and Reason is correct
- (3) Assertion is false and Reason is correct
- (4) Assertion is false and Reason is false

Answer (2)

Sol. Isothermal PV = Constant

$$\frac{dP}{DV} = -\frac{P}{V}$$

$$dP = -\frac{P}{V}(dV)_{isothermal} \qquad \dots (i)$$

Adiabatic $PV^{\gamma} = Constant$

$$\frac{dP}{dV} = -\gamma \frac{P}{V}$$

$$dP = -\frac{\gamma P}{V} (dV)_{\text{adiabatic}} \qquad \dots \text{(ii)}$$

If dP is same in both process

$$(dV)_{isothermal} = \gamma (dV)_{adiabatic}$$

- 8. Two planet A and B are revolving around a massive star such that $r_A = 2r_B$ and $m_A = 4\sqrt{3} m_B$. Find ratio of angular momentum of planet B to planet A.
 - (1) 8√3
- (2) $\frac{1}{8\sqrt{3}}$
- (3) $\frac{1}{2\sqrt{3}}$
- (4) $\frac{1}{3\sqrt{2}}$

Answer (2)



Sol. L = mvr

$$L = m\sqrt{\frac{GM}{r}}r$$

 $L = m\sqrt{GMr}$

$$\frac{L_B}{L_A} = \frac{1}{4\sqrt{3}} \cdot \frac{1}{2} = \frac{1}{8\sqrt{3}}$$

- 9. A capacitor C_1 = 6 μ F, initially charged with a cell of emf 5V is disconnected and connected to another capacitor C_2 = 12 μ F which is initially neutral. The charges on C_1 and C_2 after connection are
 - (1) 0 μC, 30 μC
- (2) 10 μC, 20 μC
- (3) 20 μC, 10 μC
- (4) 30 μC, 0 μC

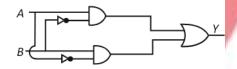
Answer (2)

Sol. Potential difference at equilibrium

$$V = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2} = \frac{(6\mu\text{F})(5\text{ V})}{(6\mu\text{F}) + (12\mu\text{F})} = \frac{5}{3}\text{ V}$$

$$q_1 = C_1 V = (6 \mu F) \left(\frac{5}{3} V \right) = 10 \mu C$$

10. The truth table for the logical circuit shown below is



- A B Y
 0 0 0
 0
 1 0 1 0
 1 0 0
 1 1 1
- A B Y
 0 0 0
 0
 1 1 1
 1 0 1
 1 1 0
- A B Y 0 0 0 0 1 1 1 1 0 1

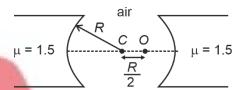
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Answer (2)

Sol.
$$Y = AB + BA$$

This is a XOR gate

11. Figure shows two spherical surfaces of radius R having common centre. If the object is placed at O, find the distance between the first images formed by both the surfaces



- (1) $\frac{4R}{35}$
- (2) $\frac{4R}{27}$
- (3) $\frac{4R}{70}$
- (4) $\frac{2R}{35}$

Answer (1)

Sol. For right surface

$$\frac{1.5}{V_1} - \frac{1}{-R/2} = \frac{0.5}{-R}$$

$$\frac{1.5}{v_1} = \frac{-2}{R} - \frac{0.5}{R}$$

$$v_1 = \frac{-3R}{5}$$

For left surface

$$\frac{1.5}{v_2} - \frac{1}{\frac{3R}{2}} = \frac{0.5}{-R}$$

$$v_2 = \frac{-9R}{7}$$

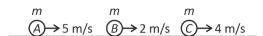
$$d=2R-\left(\frac{3R}{5}+\frac{9R}{7}\right)$$

$$d = \frac{4R}{35}$$

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 Three particles of same mass are moving a shown. (all collisions are elastic)



- S_1 : After all collisions velocities are 4 m/s, 2 m/s and 5 m/s.
- S_2 : Velocities are get interchanged in elastic collision of same mass.
- (1) S₁: Correct, S₂: Correct
- (2) S₁: Incorrect, S₂: Correct
- (3) S_1 : Incorrect, S_2 : Incorrect
- (4) S₁: Correct, S₂: Incorrect

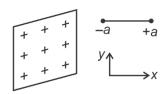
Answer (2)

- **Sol.** Aster 1st collision
 - $(A) \rightarrow 2 \text{ m/s}$
- $(B) \rightarrow 5 \text{ m/s}$
- $\bigcirc \rightarrow 4 \text{ m/s}$
- After 2nd collision
- $(A) \rightarrow 2 \text{ m/s}$
- $(B) \rightarrow 4 \text{ m/s}$
- $(C) \rightarrow 5 \text{ m/s}$
- An electromagnetic wave propagates in +X-direction.
 Then, electric field and magnetic field are directed along
 - (1) X, Y
 - (2) *Y, Z*
 - (3) Z, Y
 - (4) Y, X

Answer (2)

Sol. $\hat{C} = \hat{E} \times \hat{B}$

14. A dipole is placed such that its axis is perpendicular to the infinite charged sheet. Select the correct options



- (a) $T_{\text{net}} = 0$, F_{net} is along -ve x-axis
- (b) $T_{\text{net}} = 0$, $U = \min$
- (c) $T_{\text{net}} = 0$, $F_{\text{net}} = 0$
- (d) T_{net} and U both are maximum
- (1) (a), (b), (c) and (d)
- (2) (b) and (c)
- (3) (a) and (c)
- (4) (b) and (d)

Answer (2)

Sol.
$$T = \vec{P} \times \vec{E} = PE \sin \theta = 0$$

$$U = -\vec{P} \cdot \vec{E} = -PE$$

$$T = 0, U = \min$$

$$F_{\text{net}} = 0$$

- 15. A cup of coffee take a time 't' to cool from 90°C to 80°C in a surrounding of 20°C. If a similar cup of coffee is cooled from 80°C to 60°C in the same surrounding, it takes a time
 - (1) $\frac{13t}{5}$
 - (2) $\frac{5t}{13}$
 - (3) $\frac{12t}{5}$
 - (4) 2t

Answer (1)



Sol. From Newtons law of cooling

$$-\frac{\theta_2-\theta_1}{t}=C\left(\frac{\theta_2+\theta_1}{2}-\theta_s\right)$$

$$\Rightarrow -\left(\frac{80^{\circ}\text{C} - 90^{\circ}\text{C}}{t}\right) = C\left(\frac{90^{\circ}\text{C} + 80^{\circ}\text{C}}{2} - 20^{\circ}\text{C}\right)$$

$$\frac{10^{\circ}\text{C}}{t} = C(65^{\circ}\text{C})$$

$$C = \frac{2}{13t}$$

Also,

$$-\left(\frac{60^{\circ}C - 80^{\circ}C}{t'}\right) = C\left(\frac{60^{\circ}C + 80^{\circ}C}{2} - 20^{\circ}C\right)$$

$$\frac{20^{\circ}\text{C}}{t'} = C(50^{\circ}\text{C})$$

$$C = \frac{2}{5t'}$$

$$\frac{2}{13t} = \frac{2}{5t}$$

$$t'=\frac{13t}{5}$$

16.

17.

18.

19.

20.

SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. A converting lens of focal length 24 cm, made of glass $(\mu_{glass} = 1.5) \ \ \text{is} \ \ \text{immersed} \ \ \text{completely} \ \ \text{in} \ \ \text{water}$ $(\mu_{water} = 1.33). \ \text{It will now behave like a converging lens of}$ focal length _____ cm.

Answer (96)

Sol.
$$f_{\text{air}}(\mu_{\text{glass}-1}) = f_{\text{water}}\left(\frac{\mu_{\text{glass}}}{\mu_{\text{water}}} - 1\right)$$

$$(+24 \text{ cm}) (1.5-1) = f_{\text{water}} \left(\frac{1.5}{1.33} - 1 \right)$$

$$24 \times \frac{1}{2} = f \times \frac{1}{8}$$

$$f = 12 \times 8$$

$$f_{\text{water}} = 96 \text{ cm}$$

22. Find the number of spectral lines in H-atom when deexcite from n = 4 to ground state

Answer (6)

Sol. Number =
$$3 \times 2$$

= 6

23. For a certain mechanical system the rate of accretion $\frac{dr}{dt}$

is proportional to \sqrt{v} , where m is mass, t is time and v is velocity, then the power is proportional to $v^{n/2}$ where n is

Answer (5)

Sol.
$$F = \left(\frac{dm}{dt}\right)v = \left(R\sqrt{v}\right)v = Rv^{3/2}$$

$$P = Fv = (Rv^{3/2})v = Rv^{5/2}$$

24.

25.

CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer:

- Which one of the following forms most stable carbocation?
 - (1) (Ph)₃C-Br
 - (2) C₆H₅CH₂Br
 - (3) C₆H₅CH(Br)CH₃
 - (4) CH₃CH₂CH₂CH₂Br

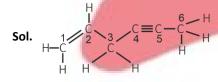
Answer (1)

Sol. $(Ph)_3C$ - Br Forms $Ph - \overset{\oplus}{C} - Ph$ as the most stable $\overset{\oplus}{Ph}$

intermediate among the given compounds.

- 2. Number of σ and π bonds respectively in hex-1-en-4- yne are
 - (1) 13, 3
- (2) 14, 3
- (3) 3, 14
- (4) 14, 13

Answer (1)



Hex-1-en-4-yne

 \Rightarrow 13 σ and 3 π bonds

- Which element in group 15 has the lowest Ionisation Energy
 - (1) Bi

(2) P

(3) As

(4) Sb

Answer (1)

4. Which of the following ether react with HBr to form phenol?

(4)
$$Ph - CH_2 - O - CH_2 - Ph$$

Answer (3)

Sol.
$$Ph-O-C$$
 CH_3 HBr $Ph-OH + Br-C-CH_3$ (via S_N1) CH_3

Consider the following thermochemical reactions and choose the correct option.

 $C(diamond) \rightarrow C(graphite) + x KJ$

C(diamond) + $O_2 \rightarrow CO_2 + y KJ$

C(graphite) + $O_2 \rightarrow CO_2 + z KJ$

- (1) x = y + z
- (2) x = y z
- (3) x + y = z
- (4) x + y = -3

Answer (2)



Sol. (1) C(diamond) \rightarrow C(graphite) $\Delta H_1 = -xkJ$

(2) C(diamond) + $O_2(g) \rightarrow CO_2(g) \Delta H_2 = -ykJ$

(3) C(graphite) + $O_2(g) \rightarrow CO_2(g) \Delta H_3 = -zkJ$ From (1), (2) and (3), we get

$$\Delta H_1 = \Delta H_2 - \Delta H_3$$

$$-x = -y + z$$

$$x = y - z$$

- 6. Which of the following will give azo dye test?
 - (1) Aniline
- (2) Anisole
- (3) Benzene
- (4) Benzaldehyde

Answer (1)

Sol.
$$N_2CI + N_2CI +$$

- 7. Which of the following is an essential amino acid?
 - (1) Alanine
- (2) Glycine
- (3) Valine
- (4) Aspartic acid

Answer (3)

- **Sol.** Tryptophan, Threonine, Histidine, Valine, Isoleucine, Phenylalanine, Methionine, Arginine, Leucine and Lysine are essential amino acids.
- 8. A drug becomes ineffective when it decomposes to 50 % its concentration. If 16 mg of said drug becomes 4 mg in 12 months, find the time in which drug becomes ineffective given that decomposition of drug follows first order kinetics.
 - (1) 6 months
- (2) 3 months
- (3) 2 months
- (4) 12 months

Answer (1)

Sol. Drug $\xrightarrow{1^{st} \text{ order}}$ Products

Initial mass of drug = 16 mg

Mass of drug after 12 months = 4 mg

 $t_{3/4} = 12$ months

 $2t_{1/2} = 12 \text{ months}$

 $t_{1/2} = 6$ months

- .. Drug becomes ineffective in 6 months.
- 9. Which of the following gives O₂ predominantly on electrolysis among the following?
 - A. Aq. AgNO₃ (Pt electrodes)
 - B. Aq. AgNO₃ (Ag electrodes)
 - C. Conc. H₂SO₄ (Pt electrodes)
 - D. Dilute H₂SO₄ (Pt electrodes)
 - (1) A, B only
 - (2) B, C only
 - (3) A, B, C only
 - (4) A, D only

Answer (4)

Sol. Aq. AgNO₃ (Pt electrodes)

Cathode: $Ag^+ + e^- \rightarrow Ag$

Anode: $2H_2O \rightarrow O_2 + 4H^+ + 4e^-$

Dilute H₂SO₄ (Pt electrodes)

Cathode: $2H_2O + 2e^- \rightarrow H_2 + OH^-$

Anode: $2H_2O \rightarrow O_2 + 4H^+ + e^-$

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Determine the type of oxide formed by an element (A)
 which has the smallest size among following.

Li, Na, K, Be, B, Mg

- (1) A₂O₃
- (2) AO
- (3) AO₂
- (4) A₂O₂

Answer (1)

- **Sol.** Among the given elements, boron (A) has the smallest size. The oxide of A is A_2O_3 .
- 11. **Statement-I:** In partition chromatography a thin film of liquid acts as stationary phase.

Statement-II: Paper chromatography is not a type of partition chromatography.

- (1) Statement-I is correct and statement-II is incorrect
- (2) Statement-I is incorrect and statement-II is correct
- (3) Both statement-I and statement-II are correct
- (4) Both statement-I and statement-II are incorrect

Answer (1)

- **Sol.** Paper chromatography is a type of partition chromatography, in which liquid acts as stationary phase.
- 12. 7.3g Benzalacetone is synthesized from 10.6 g of benzaldehyde using acetone as other reactant. Percentage yield of Benzalacetone is
 - (1) 50%
 - (2) 27%
 - (3) 90%
 - (4) 40%

Answer (1)

Sol. $C_6H_5CHO + CH_3COCH_3 \xrightarrow{Base} C_6H_5 - CH = CH - C - CH_3$ 1 mole
1 mole
(106 g)
(146 g)

10.6 g should give 14.6 g for 100% yield

10.6 g give 7.3 of Benzalacetone in this question. So, percentage yield = $\frac{7.3}{14.6} \times 100 = 50\%$

- 13. Some substances can effectively convert heat energy to electrical energy. For the conversion of thermal energy to electrical energy, the substance should have:
 - (1) Low thermal and low electrical conductivity
 - (2) High thermal and high electrical conductivity
 - (3) High thermal and low electrical conductively
 - (4) Low thermal and high electrical conductivity

Answer (4)

- **Sol.** Substance should have low thermal and high electrical conductivity as it should readily conduct electricity while poorly transferring heat.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.



SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. 0.41 g of BaSO₄ is obtained from 0.2 g of organic compound in Carius method. What is the percentage of sulphur present in organic compound?

Answer (28)

Sol. Moles of BaSO₄ =
$$\frac{0.41}{233}$$
 mol

Mass of sulphur =
$$\frac{0.41}{233} \times 32 \text{ g}$$

= 0.056 g

% of sulphur in organic compound =
$$\frac{0.056}{0.2} \times 100$$

22. The number of benzenoid structural isomers having molecular formula C_9H_{12} which do not give Baeyer's reagent test is ?

Answer (8)

Sol. D.U. =
$$\frac{18 + 2 - 12}{2} = 4$$

Baeyer's Reagent (cold dil. KMnO₄) reacts with alkene and alkynes and not with benzene.

23. How many maximum spectral lines are observed when a sample of hydrogen atoms de-excited from n = 4 to n = 1?

Answer (6)

Sol. Maximum number of spectral lines = $\frac{n(n-1)}{2}$ = $\frac{4(4-1)}{2} = \frac{12}{2} = 6$

24. Find number of non-bonding electron in NO_2^- ion is _____.

Answer (12)

Sol. O. N. O.O.

Number of non-bonding electrons will be
= 4 + 2 + 6
= 12

25. Find spin only magnetic moment of yellow coloured complex compound
K₃[Co(NO₂)₆], Cu₂[Fe(CN)₆], Zn₂[Fe(CN)₆], Cu₃[Fe(CN)₆]₂

Answer (0)

Sol. $Cu_2[Fe(CN)_6] = Chocolate brown ppt$ $Zn_2[Fe(CN)_6] = White ppt$ $Cu_3[Fe(CN)_6]_2 = Green ppt$ $K_3[Co(NO_2)_6] = Yellow ppt$ In $K_3[Co(NO_2)_6]$, Co^{3+} with $SFL(NO_2^-)$ has electronic configuration $t_{2g}^6 eg^0$

Number of unpaired $e^- = 0$

So,
$$\mu = 0$$

MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

- If the letters of the word "KANPUR" are arranged in dictionary, then the 440th word is
 - (1) PRKAUN
 - (2) PRKUAN
 - (3) PRKNAU
 - (4) PRKUNA

Answer (1)

Sol. AKNPRU

438

PRKANU \rightarrow 439th

 $PRKAUN \rightarrow 440^{th}$

- 2. Let $f(x) = \int_0^x t(t^2 3t + 20)dt$, $x \in (1,3)$ and range of f(x) is (α, β) , then $\alpha + \beta$ is equal to
 - (1) $\frac{185}{1}$
- (2) $\frac{185}{2}$
- (3) $\frac{185}{3}$
- (4) $\frac{37}{4}$

Answer (2)

Sol.
$$f(x) = \frac{x^4}{4} - x^3 + 10x^2$$

$$f'(x) = x^3 - 3x^2 + 20x$$
$$= x(x^2 - 3x + 20)$$

in (1, 3) f'(x) is positive

 \therefore f(x) is increasing in (1, 3)

$$\therefore \quad \alpha = f(1) = \frac{37}{4}$$

$$\beta = f(3) = 83.25 = \frac{333}{4}$$

$$\therefore \quad \alpha + \beta = 92.5 = \frac{185}{2}$$

3. The value of the limit

$$\lim_{x\to 0} \left(\csc x\right) \left(\sqrt{2\cos^2 x + 3\cos x} - \sqrt{\cos^2 x + \sin x + 4}\right) \text{ is }$$

(1) 0

- (2) 1
- (3) $\frac{1}{2\sqrt{5}}$
- (4) $-\frac{1}{2\sqrt{5}}$

Answer (4)

Sol. After rationalization,

$$\lim_{x \to 0} \frac{1}{\sin x} \left(\frac{\left(2\cos^2 x + 3\cos x\right) - \left(\cos^2 x + \sin x + 4\right)}{\sqrt{2\cos^2 x + 3\cos x} + \sqrt{\cos^2 x + \sin x + 4}} \right)$$

$$\lim_{x\to 0} \frac{\cos^2 x + 3\cos x - \sin x - 4}{\left(\sin x\right)\left(\sqrt{5} + \sqrt{5}\right)}$$

$$= \lim_{x \to 0} \frac{1}{2\sqrt{5}} \frac{\cos^2 x + 3\cos x - \sin x - 4}{\sin x}$$

L'Hopital,

$$\Rightarrow \lim_{x \to 0} \left(\frac{1}{2\sqrt{5}} \right) \left(\frac{2\cos x(-\sin x) - 3\sin x - \cos x}{\cos x} \right)$$

$$= \frac{1}{2\sqrt{5}} \left[\frac{-1}{1} \right] = -\frac{1}{2\sqrt{5}}$$



- 4. Let the line L be $\frac{x-1}{1} = \frac{y-4}{3} = \frac{z-7}{5}$ and foot of perpendicular from (1, -2, -1) to L is (α, β, γ) , then $\alpha + \beta + \gamma$ is
 - (1) $-\frac{69}{35}$
- (2) $\frac{102}{35}$
- (3) $\frac{69}{35}$
- (4) $-\frac{102}{35}$

Answer (4)

Sol.
$$\frac{x-1}{1} = \frac{y-4}{3} = \frac{z-7}{5} = \lambda$$

Point on line $A(\lambda + 1, 3\lambda + 4, 5\lambda + 7)$

$$B(1, -2, -1)$$

$$\overrightarrow{AB} \cdot \langle 1, 3, 5 \rangle = 0$$

$$\lambda \cdot 1 + 3(3\lambda + 6) + 5(5\lambda + 8) = 0$$

$$35\lambda + 18 + 40 = 0$$

$$\lambda = -\frac{58}{35}$$

$$(\alpha, \beta, \gamma) = \left(-\frac{23}{35}, -\frac{34}{35}, -\frac{9}{7}\right)$$

$$\alpha + \beta + \gamma = -\frac{102}{35}$$

- 5. If the exhaustive values of a for which the equation $2x^2 + (\alpha 5)x + 15 = 3\alpha$ has no real roots is (α, β) , then $|4(\alpha + \beta)|$ is equal to
 - (1) 56

(2) 52

(3) 54

(4) 18

Answer (1)

Sol. No real roots ⇒ discriminant is negative

$$\Rightarrow (a-5)^2 - 4(2) (15-3a) < 0$$

$$\Rightarrow a^2 - 10a + 25 - 120 + 24a < 0$$

$$a^2 + 14a - 95 < 0$$

$$(a + 19)(a - 5) < 0$$

$$\Rightarrow a \in (-19, 5)$$

$$\alpha = -19$$

$$\alpha = 5$$

$$|4(\alpha + \beta)|$$

- 6. Area enclosed between the curves $|y| = 1 x^2$ and $x^2 + y^2 = 1$ is $(\pi \alpha)$ sq. units, then 9α is
 - (1) 8

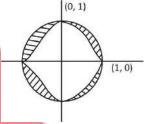
(2) 16

(3) 32

(4) 24

Answer (2)

Sol.



Area =
$$\pi - 4 \int_{0}^{1} (1 - x^{2}) dx$$

$$=\pi-4\left[x-\frac{x^3}{3}\right]_0^1$$

$$=\pi-4\times\frac{2}{3}=\left(\pi-\frac{8}{3}\right)$$
sq unit

$$=\pi-\alpha$$

$$\Rightarrow \pi = \frac{8}{3}$$

$$9\alpha = 16$$

7. If $\log y = x \log \frac{2}{5}$, $x \in \mathbb{N} \cup \{0\}$. Then sum of all values of

y equals to

- (1) $\frac{5}{3}$
- (2)

(3) $\frac{5}{4}$

(4) $\frac{8}{3}$

Answer (1)

Sol.
$$\log y = x \log \frac{2}{5}$$

$$\log y = \log \left(\frac{2}{5}\right)^x$$

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$$y = \left(\frac{2}{5}\right)^x$$

 $x \in \mathbb{N} \cup \{0\}$

$$\Rightarrow$$
 y = 1, $\frac{2}{5}$, $\left(\frac{2}{5}\right)^2$... which is in G.P.

Sum of all values of $\sum y = \frac{1}{1 - \frac{2}{5}} = \frac{5}{3}$

- 8. There is an arithmetic progression a_1 , a_2 , a_3 , ... a_{2024} and $a_1 + (a_5 + a_{10} + a_{15} ... a_{2020}) + a_{2024} = 2233$. Find the value of $a_1 + a_2 + a_3 + ... a_{2024}$.
 - (1) 11034
- (2) 11132
- (3) 10432
- (4) 20462

Answer (2)

Sol. : $a_1, a_2, a_3, ..., a_{2024}$ are in A.P.

Then $a_1 + a_{2024} = a_2 + a_{2023} = ... = a_r + a_{2024} - r + 1 = I$

$$\therefore a_1 + (a_5 + a_{10} + \dots + a_{2020}) + a_{2024} = 2023$$

or,
$$(202I) + I = 2023$$

or, 203/ = 2233

$$\therefore$$
 $a_1 + a_2 + ... + a_{2024} = 1012 \times I$

$$=1012\times\frac{2233}{203}$$

- = 1012×11
- = 11132
- 9. Two points (4, 2) and (0, 2) lie on the circle whose centre lies on 3x + 2y + 2 = 0, then length of chord whose mid point is (1, 2), is
 - (1) $\sqrt{3}$
- (2) √5
- (3) $2\sqrt{3}$
- (4) 2√5

Answer (3)

Sol. Let the centre be $(-2\alpha, 3\alpha - 1)$

$$\sqrt{(-2\alpha-4)^2+(3\alpha-3)^2} = \sqrt{(-2\alpha-0)^2+(3\alpha-3)^2}$$

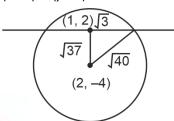
- \Rightarrow $(-2\alpha 4)^2 = (-2\alpha)^2$
- \Rightarrow $-2\alpha 4 = -2\alpha$
- ⇒ No solution

$$-2\alpha - 4 = -2\alpha$$

$$\Rightarrow \alpha = -1$$

Centre will be (2, -4), radius $\sqrt{4+36} = \sqrt{40}$

$$(x-2)^2 + (y+4)^2 = 40$$



⇒ Length of chord = $2\sqrt{3}$

10. If
$$\lim_{t\to 0} \left(\int_0^1 (3x+5)^t dx\right)^{\frac{1}{t}} = \frac{\alpha\left(\frac{8}{5}\right)^{\frac{p}{q}}}{4e}$$
, then α is

(1) 32

(2) 16

(3) 8

(4) 64

Answer (1)

Sol. Since,
$$\int_{0}^{1} (3x+5)^{t} dx = \frac{8^{t+1}-5^{t+1}}{3(t+1)}$$

$$\Rightarrow L = \lim_{t \to 0} \left(\frac{8^{t+1} - 5^{t+1}}{3(t+1)} \right)^{\frac{1}{t}}$$

$$\Rightarrow L = \lim_{t \to 0} (1 + f(t)) \frac{1}{f(x)} \cdot \frac{f(t)}{t}$$

Where
$$f(t) = \frac{8^{t+1} - 5^{t+1}}{3(t+1)} - 1 = \frac{8^{t+1} - 5^{t+1} - 3t - 3}{3(t+1)}$$

$$\Rightarrow$$
 Since, $\lim_{t\to 0} f(t) = 0$

$$L = \lim_{t \to 0} e^{\frac{f(t)}{t}} = e^{\lim_{t \to 0} \frac{f(t)}{t}} = e^{\lim_{t \to 0} f'(t)}$$

$$f'(t) = \frac{8.8^t \ln 8 - 5.5^t \ln 5 - 3}{3(t+1)} - \frac{8^{t-1} - 5^{t+1} - 3t - 3}{3(t+1)^2}$$

$$\lim_{t\to 0} f'(t) = \frac{8\ln 8 - 5\ln 5 - 3}{3} = \frac{1}{3}\ln\left(\frac{8^8}{5^5}\right) - 1$$



$$L = e^{\ln\left(\frac{8^8}{5^5}\right)^{\frac{1}{3}} - 1} = \left(\frac{8^8}{5^5}\right)^{\frac{1}{3}} \cdot e^{-1} = \frac{\left(\frac{8^8}{5^5}\right)^{\frac{1}{3}}}{e}$$

$$=\frac{1}{e}\left(\frac{8}{5}\right)^{\frac{5}{3}}.8^{\frac{1}{3}}=\frac{32\left(\frac{8}{5}\right)^{\frac{5}{3}}}{4e}$$

$$\Rightarrow \alpha$$
 = 32

11. The value of
$$\int_{0}^{\frac{\pi}{4}} \left(\sin \left| \left(4x - \frac{\pi}{2} \right) \right| + \sin[2x] \right) dx$$
 is

(where [·] denotes the greatest integer function)

(1)
$$\frac{1}{2} + \left(\frac{\pi - 2}{4}\right) \sin 1$$

(2)
$$\frac{1}{4} + \left(\frac{\pi - 2}{2}\right) \sin 1$$

(3)
$$\frac{1}{2} - \left(\frac{\pi - 2}{4}\right) \sin 1$$
 (4) $\frac{1}{4} - \left(\frac{\pi - 2}{2}\right) \sin 1$

(4)
$$\frac{1}{4} - \left(\frac{\pi - 2}{2}\right) \sin 2$$

Answer (1)

Sol.
$$\int_{0}^{\frac{\pi}{4}} \left(\sin \left| 4x - \frac{\pi}{2} \right| + \sin[2x] \right) dx$$

$$= \int_{0}^{\frac{\pi}{4}} \sin \left| 4x - \frac{\pi}{2} \right| dx + \int_{0}^{\frac{\pi}{4}} \sin[2x] dx$$

$$= \int_{0}^{\frac{\pi}{8}} \sin \left| \frac{\pi}{2} - 4x \right| dx + \int_{\frac{\pi}{8}}^{\frac{\pi}{4}} \sin \left[4x - \frac{\pi}{2} \right] dx + \int_{0}^{\frac{1}{2}} 0 dx$$

$$+\int_{\frac{1}{2}}^{\frac{\pi}{4}}\sin(1)dx$$

$$= \int_0^{\frac{\pi}{8}} \cos 4x dx + \int_{\frac{\pi}{8}}^{\frac{\pi}{4}} \cos 4x dx + \sin 1 \cdot \left(\frac{\pi}{4} - \frac{1}{2}\right)$$

$$= \left[\frac{\sin 4x}{4}\right]_0^{\frac{\pi}{8}} - \left[\frac{\sin 4x}{4}\right]_{\frac{\pi}{2}}^{\frac{\pi}{4}} + \frac{(x-2)\sin 1}{4}$$

$$= \frac{1}{4} + \frac{1}{4} + \frac{(\pi - 2)\sin 1}{4}$$

$$= \frac{(\pi - 2)\sin(1) + 2}{4} = \frac{1}{2} + \left(\frac{\pi - 2}{4}\right)\sin 1$$

- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.

SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. Let
$$a_{ij} = \left(\sqrt{2}\right)^{i+j}$$
, $A = \left[a_{ij}\right]_{3\times 1}$. If sum of third row of A^2 is $\alpha + \beta\sqrt{2}$, then $\alpha + \beta$ is

Answer (224)

Sol.
$$\begin{bmatrix} 2 & 2\sqrt{2} & 4 \\ 2\sqrt{2} & 4 & 4\sqrt{2} \\ 4 & 4\sqrt{2} & 8 \end{bmatrix} \begin{bmatrix} 2 & 2\sqrt{2} & 4 \\ 2\sqrt{2} & 4 & 4\sqrt{2} \\ 4 & 4\sqrt{2} & 8 \end{bmatrix} = \begin{bmatrix} 28 & 28\sqrt{2} & 56 \\ 28\sqrt{2} & 56 & 56\sqrt{2} \\ 56 & 56\sqrt{2} & 112 \end{bmatrix}$$

$$56 + 112 + 56\sqrt{2}$$

$$168 + 56\sqrt{2}$$

$$\alpha + \beta \sqrt{2}$$

$$\alpha + \beta = 224$$

22. If 3^{107} is divided by 23, then remainder is

Answer (06)

Sol. Notice that, $3^4 \equiv (12) \pmod{23}$

$$\Rightarrow$$
 3⁸ = 144 = 6(mod 23)

$$3^{11} \equiv 1 \pmod{23}$$

$$(3^{11})^9 \equiv 1 \pmod{23}$$

$$3^{99} \equiv 1 \pmod{23}$$

$$3^8 \cdot 3^{99} \equiv 1 \pmod{23}$$

$$\Rightarrow 3^{107} \equiv 6 \pmod{23}$$

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23. If α , β are the values of m where

$$x + y + 2z = 1$$

$$x + 2y + 4z = m$$

 $x + 4y + 8 = m^2$ have infinitely many solutions.

Then
$$\sum_{n=1}^{10} (n^{\alpha} + n^{\beta})$$
 is equal to

Answer (440)

Sol. For infinite solution

$$\Delta = \Delta_1 = \Delta_2 = \Delta_3 = 0$$

$$\Delta = \begin{vmatrix} 1 & 1 & 2 \\ 1 & 2 & 4 \\ 1 & 4 & 8 \end{vmatrix} = 0$$

$$\Delta_1 = \begin{vmatrix} 1 & 1 & 2 \\ m & 2 & 4 \\ m^2 & 4 & 8 \end{vmatrix} = 0$$

$$\Delta_2 = \begin{vmatrix} 1 & 1 & 2 \\ 1 & m & 4 \\ 1 & m^2 & 8 \end{vmatrix} = 0 \implies m^2 + 3m - 2$$

$$\Rightarrow m^2 - 3m + 2 = 0$$

$$m = 2, 1$$

$$\Delta_3 = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 2 & m \\ 1 & 4 & m^2 \end{vmatrix} = 0 \implies m^2 - 3m + 2 = 0$$

$$\Rightarrow$$
 $m = 2, 1 \Rightarrow \alpha = 1, \beta = 2$

$$\sum_{n=1}^{10} (n)^{1} + (n)^{2} = \frac{10 \times 11}{2} + \frac{10 \times 11 \times 21}{6}$$

- = 440
- 24. If the domain of $\log_{x-1} \left(\frac{2x^2 9x + 4}{x^2 4x + 5} \right)$ is (α, ∞) and

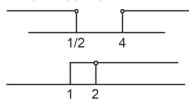
 $\log_5(18x - x^2 - 77)$ is (β, γ) , then the value of $\alpha^2 + \beta^2 + \gamma^2$ is

Answer (186)

Sol.
$$\frac{2x^2-9x+4}{x^2-4x+5} > 0$$
 ...(i)

$$x-1 > 0, x-1 \neq 1$$

$$\Rightarrow$$
 $(2x-1)(x-4)>0$



$$\therefore x \in (4, \infty)$$

$$\alpha = 4$$

$$\log_5(18x - x^2 - 77)$$

$$\Rightarrow$$
 18x - x² - 77 > 0

$$\Rightarrow x^2 - 18x + 77 < 0$$

$$\Rightarrow$$
 $(x-7)(x-11)<0$

$$x \in (7, 11)$$

$$\beta = 7, \gamma = 11$$

$$\alpha^2 + \beta^2 + \gamma^2$$

25. The equation $\alpha x + \beta y = 109$ is chord of ellipse

$$\frac{x^2}{9} + \frac{y^2}{4} = 1$$
 having midpoint $\left(\frac{5}{2}, \frac{1}{2}\right)$, then $\alpha + \beta$ is

Answer (58)

Sol. Chord with given middle point

$$T = S_1$$

$$\frac{5}{18}x + \frac{y}{8} = \frac{25}{36} + \frac{1}{16} = \frac{109}{144}$$

$$40x + 18y = 109$$

$$\equiv \alpha x + \beta y = 109$$

$$\Rightarrow \alpha = 40$$
 $\beta = 18$

$$\alpha + \beta = 58$$