

## Solutions

**S1.** Ans. (d)

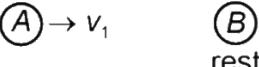
$$x = 2t - 1$$

$$v = \frac{dx}{dt} = 2m\ s^{-1}$$

$$P = F \cdot v$$

$$= 2 \times 5 = 10\ W.$$

**S2.** Ans. (a)

Before collision  $\Rightarrow$  

It undergoes completely inelastic collision

Using conservation of linear momentum

Initial momentum = Final momentum.

$$\Rightarrow mv_1 = mv_2 + mv_2$$

$$\Rightarrow mv_1 = 2mv_2$$

$$\Rightarrow \frac{v_1}{v_2} = \frac{2}{1}.$$

**S3.** Ans. (a)

Potential energy stored in the spring

$$= \frac{1}{2}kx^2$$

$$\text{Now } \frac{1}{2}k(2)^2 = U$$

$$\& \frac{1}{2}k(8)^2 = U' \quad (\text{say})$$

$$\Rightarrow U' = \frac{64}{4}U = 16U$$

**S4.** Ans. (b)

$$\frac{1}{2}m\left(\frac{u}{3}\right)^2 - \frac{1}{2}mu^2 = -F_R \times 24$$

$$0 - \frac{1}{2}mu^2 = -F_R \times d$$

$$\frac{\frac{1}{2}mu^2}{\frac{1}{2}mu^2 \times \frac{8}{9}} = \frac{d}{24}$$

$$d = 24 \times \frac{9}{8} = 27\ cm$$

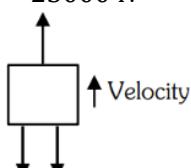
**S5.** Ans. (b)

Constant velocity  $\Rightarrow a = 0$

$$\Rightarrow T = W + f$$

$$= 20000 + 3000$$

$$= 23000\ N$$



$$\Rightarrow \text{Power} = Tv$$

$$= 23000 \times 1.5$$

$$= 34500\ \text{watts}$$

**S6.** Ans. (a)

Hint:  $E = mgh$

$$P_{\text{input}} = \frac{mgh}{t}$$

$$= \frac{15 \times 10 \times 60}{1} = 9000 = 9\ \text{kW}$$

$$10\% \text{ loss} = 0.9 \times 10^3$$

$$P_{\text{input}} = 9 \times 10^3 - 0.9 \times 10^3 = 8.1\ \text{kW}$$

**S7.** Ans. (b)

Hint: According to the given question

$$T - mg = m \frac{(\sqrt{gr})^2}{r}$$

$$\Rightarrow T = 8mg$$

**S8.** Ans. (b)

Hint: From law of conservation of momentum, we have

$$4mu_1 = 4mv_1 + 2mv_2$$

$$\Rightarrow 2(u_1 - v_1) = v_2 \dots \dots \dots (1)$$

From the law of conservation of K.E. we have

$$\frac{1}{2}4mu_1^2 = \frac{1}{2}4mv_1^2 + \frac{1}{2}2mv_2^2$$

$$\Rightarrow 2(u_1^2 - v_1^2) = v_2^2 \dots \dots \dots (2)$$

From (1) and (2),

$$2(u_1^2 - v_1^2) = 4(u_1 - v_1)^2$$

$$3v_1 = u_1$$

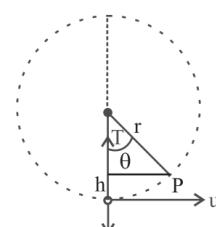
Now, fraction of loss in kinetic energy for mass  $4m$ ,

$$\frac{\Delta K}{K_i} = \frac{K_i - K_f}{K_i} = \frac{\left(\frac{1}{2}(4m)u_1^2 - \frac{1}{2}(4m)v_1^2\right)}{\frac{1}{2}(4m)u_1^2}$$

$$\therefore \frac{\Delta K}{\Delta K_i} = \frac{8}{9}$$

**S9.** Ans. (c)

Hint: Now, at point P from figure



$$T - mg \cos \theta = \frac{mv^2}{r}$$

$$\therefore T = mg \cos \theta + \frac{mv^2}{r}$$

From figure,  $\cos\theta = \frac{r-h}{r}$

So T will be maximum when  $\cos\theta$  will be 1

$$\therefore \frac{r-h}{r} = 1$$

$$\Rightarrow h = 0$$

The tension is maximum when the mass is at the lowest position of the vertical circle, so the chance of breaking is maximum.

**S10.** Ans. (c)

Hint: Work done by variable force is

$$W = \int_{y_i}^{y_f} F dy$$

$$\text{Here, } y_i = 0, y_f = 1 \text{ m}$$

$$\therefore W = \int_0^1 (20 + 10y) dy = [20y + 5y^2]_0^1 = 25 \text{ J}$$

**S11.** Ans. (d)

Hint: To complete vertical circle minimum velocity required at lowest point of circle is  $\sqrt{5gr}$  so by

$$mgh = \frac{1}{2}mv^2 \quad r = \frac{D}{2}$$

$$mgh = \frac{1}{2} m \times 5g \frac{D}{2}$$

$$h = \frac{5D}{4}$$

**S12.** Ans. (b)

Hint: Spring constant  $K \propto \frac{1}{\ell}$

Where  $\ell$  = natural length of spring

$$K = \frac{c}{\ell} = \text{constant}$$

It is cut into lengths of ratio 1 : 2 : 3 then ratio of spring constant,

$$\frac{c}{1} : \frac{c}{2} : \frac{c}{3} \Rightarrow \frac{1}{1} : \frac{1}{2} : \frac{1}{3}$$

$$K_1 : K_2 : K_3 \Rightarrow 6 : 3 : 2$$

Now,

parallel combination

$$K = 6K + 3K + 2K \Rightarrow K = 11K$$

$$\frac{1}{K'} = \frac{1}{6K} + \frac{1}{2K} + \frac{1}{3K}$$

$$\frac{1}{K'} = \frac{1}{6K} + \frac{(3+2)}{6K} \Rightarrow \frac{1}{K'} = \frac{1}{K}$$

$$K' = K$$

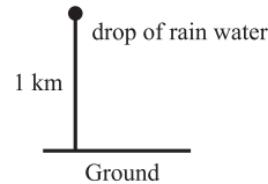
$$\frac{K'}{K''} = \frac{K}{11K} \Rightarrow \frac{K'}{K''} = \frac{1}{11}$$

**S13.** Ans. (c)

Hint: Apply work energy theorem

$$W_{\text{all force}} = K_f - K_i$$

$$W_{(\text{conservative})} + W_{(\text{non conservative})} = K_f - K_i$$



$$W_g = mgh$$

$$= 10^{-3} \times 10 \times 10^3$$

$$= 10 \text{ J}$$

$$(U_1 - U_2) + W_{fr} = \frac{1}{2}mv^2 - 0 \quad [K_i = 0, u = 0]$$

$$mgh + W_{fr} = \frac{1}{2}mv^2 \quad [U_2 = 0]$$

$$10^{-30} \times 10 \times 1000 + W_{fr} = \frac{1}{2} \times 10^{-3} \times (50)^2$$

$$10 + W_{fr} = 1.25$$

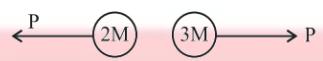
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Work done by resistive force

$$W_{fr} = -8.25 \text{ J}$$

**S14.** Ans. (d)

Hint:



$$F_{\text{ext}} = 0$$

$$\vec{P} = \text{constant}$$

$$K.E. = \frac{P^2}{2m} \Rightarrow K.E. \propto \frac{1}{m}$$

$$\therefore K.E_{2M} = \frac{3E}{5}$$

**S15.** Ans. (d)

$$\text{Hint: Power} = \frac{K.E.}{t} = \frac{\frac{1}{2}mv^2}{t}$$

$$v = \sqrt{t}$$

$$\frac{ds}{dt} = t^{\frac{1}{2}}$$

$$ds = t^{\frac{1}{2}} dt$$

$$s = \frac{2t^{\frac{3}{2}}}{3} \Rightarrow s \propto t^{\frac{3}{2}}$$

Slope of x-t graph is +ve.

**S16.** Ans. (a)

$$\text{Hint: } \vec{s} = \vec{r}_f - \vec{r}_i = 2\hat{i} - \hat{j} + 3\hat{k}$$

$$W = \vec{F} \cdot \vec{s} = (4\hat{i} + 3\hat{j}) \cdot [2\hat{i} - \hat{j} + 3\hat{k}]$$

$$= 8 - 3 = 5\text{J}$$

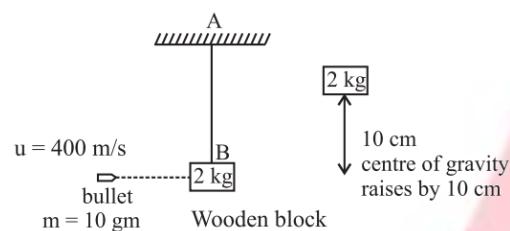
**S17.** Ans. (d)

Hint: Since both bodies are identical and collision is elastic. Therefore, velocities will be interchanged after collision.

$$v_A = -0.3 \text{ m/s and } v_B = 0.5 \text{ m/s}$$

**S18.** Ans. (a)

Hint: AB = 5 m



Apply conservation of linear momentum

$$mu + 0 = mv + Mv$$

$$\frac{10}{100} \times 400 + 0 = \frac{10}{100} v + 2V$$

$$0.01v + 2V = 4 \dots \dots \dots (1)$$

$$PE = KE$$

$$MgH = \frac{1}{2} \times MV^2$$

$$2 \times 10 \times \frac{10}{100} = \frac{1}{2} \times 2 \times V^2$$

$$\Rightarrow V^2 = 2$$

$$v = \sqrt{2} \text{ ms}^{-1}$$

Substituting the value of  $V$  in Eq. (1), we get

$$\frac{v}{100} + 2\sqrt{2} = \Rightarrow v = (4 - 2\sqrt{2})100$$

$$\simeq 120 \text{ ms}^{-1}$$

**S19.** Ans. (d)

$$\text{Hint: } \vec{F} = 2t\hat{i} + 3t^2\hat{j}$$

$$m \frac{d\vec{v}}{dt} = 2t\hat{i} + 3t^2\hat{j}$$

$$\int_0^{\bar{v}} d\bar{v} = \int_0^t (2t\hat{i} + 3t^2\hat{j}) dt = t^2\hat{i} + t^3\hat{j}$$

$$\text{Power} = \vec{F} \cdot \bar{V} = (2t^3 + 3t^5)W$$

**S20.** Ans. (c)

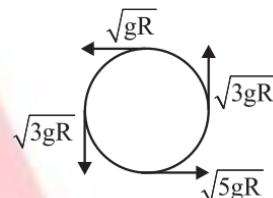
Hint: The potential energy gets converted into heat and only one quarter of it is absorbed by ice.

$$\frac{mgh}{4} = mL$$

$$h = \frac{4L}{g} = \frac{4 \times 3.4 \times 10^5}{10} = 136 \text{ km}$$

**S21.** Ans. (d)

Hint: Minimum velocity required at different points to complete full vertical circle



**S22.** Ans. (a)

$$\text{Hint: } \frac{1}{2}mv^2 = E \rightarrow \frac{1}{2}\left(\frac{10}{1000}\right)v^2 = 8 \times 10^{-4}$$

$$v^2 = (8 \times 10^{-4})200 = \frac{16}{100} \text{ ms}^{-1}$$

$$v = \frac{4}{10} \text{ ms}^{-1}$$

Now applying  $v^2 - u^2 = 2as$

$$\left(\frac{4}{10}\right)^2 = 2a(4\pi R); [s = 4\pi R = 2(2\pi R)]$$

$$\frac{16}{100} = 2a \left(4\pi \frac{6.4}{100}\right)$$

$$a = \frac{16}{100} \times \left[\frac{7 \times 100}{8 \times 22 \times 6.4}\right] = 0.1 \text{ m/s}^2$$

**S23.** Ans. (d)

Hint:  $P = Fv = mav$

$$\Rightarrow k = m \frac{dv}{dt}$$

By integrating the equation

$$\Rightarrow \int v dv = \int \frac{k}{m} dt$$

$$\Rightarrow \frac{v^2}{2} = \frac{k}{m} t \Rightarrow v = \sqrt{\frac{2kt}{m}}$$

$$a = \frac{dv}{dt} = \sqrt{\frac{2k}{m}} \left(\frac{1}{2} t^{-\frac{1}{2}}\right)$$

$$F = ma = m \left(\frac{1}{2}\right) \sqrt{\frac{2k}{m}} \Rightarrow F = \sqrt{\frac{mk}{2t}} = \sqrt{\frac{mk}{2}} t^{-\frac{1}{2}}$$

**S24.** Ans. (b)

Hint: Given  $K_P > K_Q$

Case (a) :  $x_1 = x_2 = x$

$$\frac{W_P}{W_Q} = \frac{\frac{1}{2}K_P x^2}{\frac{1}{2}K_Q x^2} = \frac{K_P}{K_Q} \Rightarrow W_P > W_Q$$

Case (b):  $F_1 = F_2 = F$

For constant force

$$W = \frac{F^2}{2K} \Rightarrow W \propto \frac{1}{K}$$

$$\text{So, } \frac{W_P}{W_Q} = \frac{K_Q}{K_P} \Rightarrow W_Q > W_P$$

**S25.** Ans. (d)

$$F = -0.1x \text{ J/m}$$

According to Work Energy theorem Work done by all force =  $K_f - K_i$

$$\int F \, dx = K_f - K_i$$

$$\int_{20}^{30} -0.1x \, dx = K_f - \frac{1}{2} \times mu^2$$

$$(-)0.1 \left[ \frac{x^2}{2} \right]_{20}^{30} = K_f - \frac{1}{2} \times 10 \times 10^2$$

$$\frac{1}{10 \times 2} [x^2]_{20}^{30} = K_f - 500$$

Limit inverse to make -ve to positive

$$\frac{1}{20} \times [400 - 900] = K_f - 500$$

$$-\frac{500}{20} = K_f - 500$$

$$K_f = 500 - 25 = 475 \text{ J}$$

**S26.** Ans. (b)

Hint: Energy will always be conserved so

$K.E_{\text{initial}} = K.E_{\text{final}} + \text{Excitation energy}$

$$\frac{1}{2}m_1u_1^2 + \frac{1}{2}m_2u_2^2 = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 + \epsilon$$

**S27.** Ans. (b)

Hint: Pressure = 150 mm Hg

$$\text{Pumping rate} = \frac{dV}{dt} = \frac{5 \times 10^{-3}}{60} \text{ m}^3/\text{s}$$

$$\text{Power of heart} = P \cdot \frac{dV}{dt} = \rho gh \times \frac{dV}{dt}$$

$$= (13.6 \times 10^3 \text{ kg/m}^3) (10) \times (0.15) \times \frac{5 \times 10^{-3}}{60}$$

$$= \frac{13.6 \times 5 \times 0.15}{6} = 1.72 \text{ watt}$$

**S28.** Ans. (b)

Hint: In elastic collision energy of system remains same

$$(K.E)_{\text{before collision}} = (K.E)_{\text{after collision}}$$

Let speed of second body after collision is  $v'$

$$\frac{1}{2}mv^2 + 0 = \frac{1}{2}m\left(\frac{v}{3}\right)^2 + \frac{1}{2}m(v')^2 \Rightarrow v' = \frac{2\sqrt{2}}{3}v$$

**S29.** Ans. (c)

Hint: Let ball rebounds with speed  $v$  so

$$v = \sqrt{2gh} = \sqrt{2 \times 10 \times 20} = 20 \text{ m/s}$$

Energy just after rebound

$$E = \frac{1}{2} \times m \times v^2 = 200 \text{ m}$$

50% energy loses in collision means just before collision energy is 400 m By using energy conservation

$$\frac{1}{2}mv_0^2 + mgh = 400 \text{ m}$$

$$\Rightarrow \frac{1}{2}mv_0^2 + m \times 10 \times 20 = 400 \text{ m}$$

$$\Rightarrow v_0 = 20 \text{ ms}^{-1}$$

**S30.** Ans. (b)

Hint: ) For two particles to collide, the direction of the relative velocity of one with respect to other should be directed towards the relative position of the other particle

i.e.  $\frac{\vec{r}_1 - \vec{r}_2}{|\vec{r}_1 - \vec{r}_2|} \rightarrow$  direction of relative position of 1 w.r.t 2

And  $\frac{\vec{v}_2 - \vec{v}_1}{|\vec{v}_2 - \vec{v}_1|} \rightarrow$  direction velocity of 2 w.r.t. 1

So for collision of A and B

$$\frac{\vec{r}_1 - \vec{r}_2}{|\vec{r}_1 - \vec{r}_2|} = \frac{\vec{v}_2 - \vec{v}_1}{|\vec{v}_2 - \vec{v}_1|}$$

**S31.** Ans. (d)

$$\text{Hint: } \vec{A} \cdot \vec{B} = 0$$

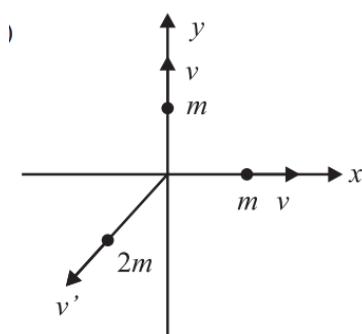
$$\cos \omega t \cos \frac{\omega t}{2} + \sin \omega t \sin \frac{\omega t}{2} = 0$$

$$\cos \left( \omega t - \frac{\omega t}{2} \right) = 0 \Rightarrow \cos \frac{\omega t}{2} = 0$$

$$\Rightarrow \frac{\omega t}{2} = \frac{\pi}{2} \Rightarrow t = \frac{\pi}{\omega}$$

**S32.** Ans. (b)

Hint:



Let

$\vec{v}'$  be velocity of third piece of mass  $2m$ .

Initial momentum,  $\vec{p}_i = 0$  (As the body is rest)

Final momentum,  $\vec{p}_f = mv\hat{i} + mv\hat{j} + 2m\vec{v}'$

According to law of conservation of momentum

$$\vec{p}_i = \vec{p}_f$$

$$= mv\hat{i} + mv\hat{j} + 2m\vec{v}'$$

$$\vec{v}' = -\frac{v}{2}\hat{i} - \frac{v}{2}\hat{j}$$

The magnitude of  $\vec{v}'$  is

$$v' = \sqrt{\left(-\frac{v}{2}\right)^2 + \left(-\frac{v}{2}\right)^2} = \frac{v}{\sqrt{2}}$$

Total kinetic energy generated due to explosion

$$= \frac{1}{2}mv^2 + \frac{1}{2}mv^2 + \frac{1}{2}(2m)v^2$$

$$= \frac{1}{2}mv^2 + \frac{1}{2}mv^2 + \frac{1}{2}(2m)\left(\frac{v}{\sqrt{2}}\right)^2$$

$$= mv^2 + \frac{mv^2}{2} = \frac{3}{2}mv^2$$

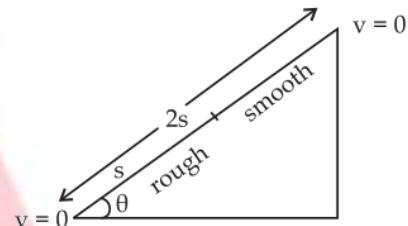
**S33.** Ans. (b)

Hint:  $W = \vec{F} \cdot \vec{S} = (3\hat{i} + \hat{j}) \cdot [(4-2)\hat{i} + (3-0)\hat{j} + (-1-1)\hat{k}]$

$$= (3\hat{i} + \hat{j}) \cdot (2\hat{i} + 3\hat{j} - 2\hat{k}) \Rightarrow 3(2) + 1(3) + 0(-2) = 9J$$

**S34.** Ans. (d)

Hint:



From Work Energy theorem ( $W = \Delta K.E$ )

$$(mg \sin \theta)(2s) - (\mu mg \cos \theta)(s) = 0 - 0$$

$$\Rightarrow \mu = 2 \tan \theta$$

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