

## Solutions

S1. Ans.(a)

$$x = 5 \sin\left(\pi t + \frac{\pi}{3}\right) m$$

Amplitude = 5 m

$$\omega = \pi$$

$$\omega = \frac{2\pi}{T}$$

$$T = \frac{2\pi}{\pi} = 2 \text{ s.}$$

S2. Ans.(a)

$$T' = 2\pi \sqrt{\frac{\ell'}{g}} \text{ where } \ell' = \frac{\ell}{2}$$

$$T = 2\pi \sqrt{\frac{\ell}{g}}$$

$$T' = \frac{X}{2} T$$

$$2\pi \sqrt{\frac{\ell}{2g}} = \frac{X}{2} 2\pi \sqrt{\frac{\ell}{g}}$$

$$\frac{1}{\sqrt{2}} = \frac{X}{2} \Rightarrow X = \sqrt{2}.$$

S3. Ans.(a)

From x - t graph

$$A = 1 \quad T = 8$$

$$\Rightarrow \omega = \frac{2\pi}{T}$$

$$\Rightarrow \omega = \frac{\pi}{4}$$

At  $t = 2, x = 1$

$$a = -\omega^2 x$$

$$\Rightarrow a = \frac{-\pi^2}{16} \times 1$$

$$\Rightarrow a = \frac{-\pi^2}{16} \text{ m/s}^2$$

S4. Ans.(d)

$$n(T)_l = (n + 1)T_s$$

$$(n)2\pi \sqrt{\frac{1.21}{g}} = (n + 1)2\pi \sqrt{\frac{1}{g}}$$

$$(n)(1.1) = (n + 1)$$

$$0.1(n) = 1$$

$$n = 10$$

No. of oscillation of smaller one

$$= n + 1$$

$$= 10 + 1$$

$$= 11$$

S5. Ans.(a)

Frequency of K.E. =  $2 \times F$

S6. Ans.(c)

$$K = \frac{10}{5 \times 10^{-2}} = 200 \text{ N/M}$$

$$T = 2\pi \sqrt{\frac{m}{k}} = \frac{\pi}{5} \text{ sec}$$

$$T = 0.628 \text{ sec}$$

S7. Ans.(d)

Displacement ( $\pi$ ) equation is

$$x = A \sin(\omega t + \phi) \quad \dots(i)$$

$$\frac{dx}{dt} = A\omega \cos(\omega t + \phi)$$

$$a = \frac{d^2x}{dt^2} = -\omega^2 A \sin(\omega t + \phi)$$

$$a = \omega^2 A \sin(\omega t + \phi + \pi) \quad \dots(ii)$$

From equation (i) and (ii) phase difference between displacement and acceleration is  $\pi$

S8. Ans.(b)

$\sin \omega t$  and  $\cos \omega t$  both are periodic function

S9. Ans.(b)

$$y = A_0 + A \sin \omega t + B \cos \omega t$$

This S.H.M can be reduced to

$$y' = y - A_0 = A \sin \omega t + B \cos \omega t$$

Hence, resultant amplitude

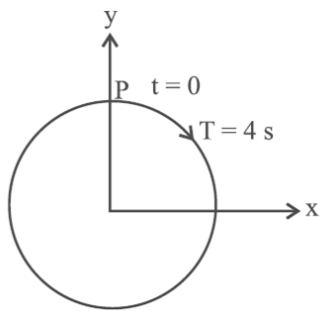
$$R = \sqrt{A^2 + B^2 + 2AB \cos 90^\circ} \\ = \sqrt{A^2 + B^2}$$

S10. Ans.(d)

In one complete vibration the displacement of the particle is zero. So, average velocity in one complete vibration =  $\frac{\text{Displacement}}{\text{Time interval}} = \frac{y_f - y_i}{T} = 0$

S11. Ans.(d)

At  $t = 0, y$  displacement is maximum, so equation will be cosine function



$$T = 4\text{ s}$$

$$\omega = \frac{2\pi}{T} = \frac{2\pi}{4} = \frac{\pi}{2} \text{ rad/s}$$

$$y = a \cos \omega t$$

$$y = 3 \cos \frac{\pi}{2} t$$

S12. Ans.(b)

$$a = \omega^2 x \Rightarrow 20 = \omega^2 5$$

$$\omega = 2$$

$$T = \frac{2\pi}{\omega} = \pi \text{ sec}$$

S13. Ans.(b)

$$\text{Acceleration} = \omega^2 x, \text{ velocity} = \omega \sqrt{A^2 - x^2}$$

$$A = 3 \text{ cm}$$

$$x = 2 \text{ cm}$$

$$a = v$$

$$\omega^2 x = \omega \sqrt{A^2 - x^2} \Rightarrow \omega x = \sqrt{A^2 - x^2}$$

$$2\omega = \sqrt{3^2 - 2^2} \Rightarrow 2\omega = \sqrt{5}$$

$$\omega = \frac{\sqrt{5}}{2} \Rightarrow \frac{2\pi}{T} = \frac{\sqrt{5}}{2}$$

$$T = \frac{4\pi}{\sqrt{5}}$$

S14. Ans.(b)

$$y_1 = a \sin \omega t$$

$$y_2 = b \cos \omega t = b \sin \left( \omega t + \frac{\pi}{2} \right)$$

Since the frequencies for both S.H.M. are same, resultant motion will be S.H.M. Now

$$\text{Amplitude } A = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos \phi}$$

$$\text{Here } A_1 = a, A_2 = b, \phi = \frac{\pi}{2}$$

$$\text{So } A = \sqrt{a^2 + b^2}$$

S15. Ans.(a)

For particle undergoing S.H.M.

$$V = \omega \sqrt{A^2 - x^2}$$

$$\text{So, } V_1 = \omega \sqrt{A^2 - x_1^2} \text{ \& } V_2 = \omega \sqrt{A^2 - x_2^2}$$

Solving these two equation, we get

$$\omega = \sqrt{\frac{V_1^2 - V_2^2}{x_2^2 - x_1^2}} = \frac{2\pi}{T} \Rightarrow T = 2\pi \sqrt{\frac{x_2^2 - x_1^2}{V_1^2 - V_2^2}}$$

S16. Ans.(a)

Two consecutive resonant frequencies for a string fixed at both ends will be

$$\frac{nv}{2l} \text{ and } \frac{(n+1)v}{2l} \Rightarrow \frac{(n+1)v}{2l} - \frac{nv}{2l} = 420 - 315$$

$$\frac{v}{2l} = 105 \text{ Hz}$$

S17. Ans.(a)

For S.H.M.

$$\text{Maximum acceleration} = \omega^2 A = \alpha$$

$$\text{Maximum velocity} = \omega A = \beta$$

$$\frac{\alpha}{\beta} = \frac{A\omega^2}{\omega A} = \omega = \frac{2\pi}{T}$$

$$\Rightarrow T = \frac{2\pi\beta}{\alpha}$$

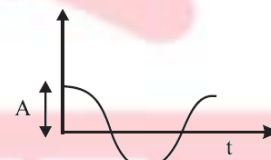
S18. Ans.(c)

$$\text{Displacement, } x = A \cos(\omega t)$$

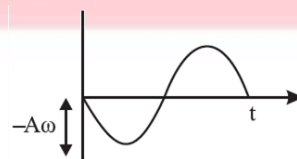
$$\text{At } t = 0$$

$$x = A \cos(\omega \times 0)$$

$$x = A$$



$$V = \frac{dx}{dt} = -A\omega \sin \omega t \text{ on comparing this with } V = V_0 \sin \omega t \quad [\because \text{sin function starts from origin}]$$



$$a = \frac{dV}{dt} = -A\omega^2 \cos \omega t$$

[ $\because$  cos function do not starts from origin]

