

Solutions

S1. Ans.(c)

Fundamental harmonic frequency open pipe = $\frac{v}{2L} = v_1$ (say)

Fundamental harmonic frequency closed pipe = $\frac{v}{4L} = v_2$ (say)

$$\Rightarrow \frac{v_1}{v_2} = \frac{\frac{v}{2L}}{\frac{v}{4L}} = 2:1$$

S2. Ans.(b)

$$v \propto \sqrt{\text{Tension}}$$

$$\frac{v_i}{v_f} = \sqrt{\frac{T_i}{T_f}}$$

$$\frac{v_i}{v_f} = \sqrt{\frac{T}{2T}}$$

$$\frac{v_i}{v_f} = \sqrt{\frac{1}{2}} = \frac{1}{\sqrt{2}}$$

S3. Ans.(a)

$$v = \frac{1}{2l} \sqrt{\frac{T}{\mu}}$$

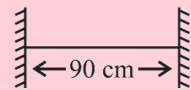
Tension decreases means frequency decreases

$$|\eta_A - \eta_B| = 6\text{Hz}$$

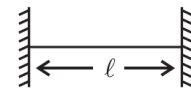
$$530\text{Hz} \begin{cases} \nearrow 536\star \\ \searrow 524\checkmark \end{cases}$$

$$|\eta_A - \eta_B^1| = 7\text{Hz}$$

S4. Ans.(a)



$$f = 120\text{Hz} = \frac{v}{2l} \Rightarrow 120 = \frac{v}{2(0.9)}$$



$$f = 180\text{Hz} = \frac{v}{2l}$$

$$\Rightarrow 180 = \frac{120 \times 0.9}{l} \Rightarrow l = 60\text{cm}$$

S5. Ans.(c)

$$\text{Open O.P.} = f_0 = \frac{v}{2l_1}$$

$$\text{Closed O.P.} = f_3 = \frac{3v}{4l_2}$$

$$\frac{v}{2l_1} = \frac{3v}{4l_2} \Rightarrow \frac{1}{l_1} = \frac{3}{2 \times 20} \quad (\because l_2 = 20)$$

$$l_1 = \frac{40}{3} = 13.33\text{ cm}$$

S6. Ans.(b)

$$\frac{\lambda}{2} = 73 - 20 = 53\text{cm}$$

$$V = f\lambda = 320 \times (53 \times 2 \times 10^{-2}) = 339.2$$

S7. Ans.(a)

In a closed organ pipe

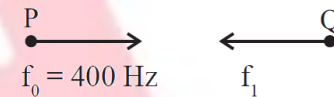
Fundamental frequency $f_0 = \frac{v}{4l}$ only odd harmonics produce so difference between any two successive harmonics

$$260 - 220 = \frac{2v}{4l}$$

$$40 = \frac{2v}{4l}$$

$$40 = 2f_0 \Rightarrow f_0 = 20\text{ Hz}$$

S8. Ans.(c)



$$v_0 = 22\text{m/s} \quad v_0 = 16.5\text{ m/s}$$

$$f_1 = f_0 \left[\frac{v+v_0}{v-v_0} \right]$$

$$f_1 = 400 \left[\frac{340+16.5}{340-22} \right]$$

$$f_1 = 448\text{ Hz}$$

S9. Ans.(d)

Shifting in wavelength $\Delta\lambda = 0.1\text{\AA}$

$$\lambda = 6000\text{\AA}$$

$$\frac{V}{c} = \frac{\Delta\lambda}{\lambda}$$

$$V = \frac{\Delta\lambda c}{\lambda}$$

$$= \frac{0.1 \times 10^{-10} \times 3 \times 10^8}{6000 \times 10^{-10}}$$

$$= 0.5 \times 10^4\text{ ms}^{-1} = 5\text{ kms}^{-1}$$

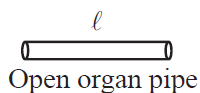
S10. Ans.(b)

$$f = \frac{v}{2l}$$

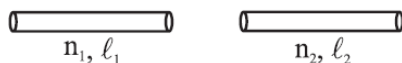
$$1.2 \times 10^3\text{ Hz} = \frac{v}{2 \times 1}$$

$$V = 2.4 \times 10^3\text{ m/s}$$

S11. Ans.(d)



$$n = \frac{v}{2l} \Rightarrow l = \frac{v}{2n}$$



$$l_1 = \frac{v}{2n_1}$$

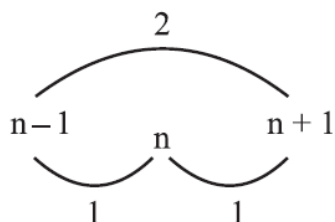
$$l_2 = \frac{v}{2n_2}$$

$$l = l_1 + l_2$$

$$\frac{v}{2n} = \frac{v}{2n_1} + \frac{v}{2n_2}$$

$$n = \frac{n_1 n_2}{n_1 + n_2}$$

S12. Ans.(b)



Beats: Max difference between two wave frequency. Therefore $(n + 1) - (n - 1) = 2$

S13. Ans.(d)

For second overtone (3rd harmonic) in open organ pipe,

$$f' = \frac{3v}{2L_{open}}$$

For first overtone (3rd harmonic) in closed organ pipe,

$$f = \frac{3v}{4L_{closed}}$$

$$f = f'$$

$$L_{open} = 2L$$

S14. Ans.(b)

$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$3 = 2\pi \sqrt{\frac{m}{k}} \quad \dots(1)$$

$$5 = 2\pi \sqrt{\frac{m+1}{k}} \quad \dots(2)$$

$$\frac{9}{25} = \frac{m}{m+1} \Rightarrow m = \frac{9}{16}$$

S15. Ans.(c)

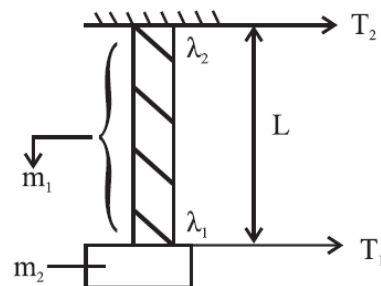
First minimum resonating length for closed organ pipe.

$$= \frac{\lambda}{4} = 50 \text{ cm}$$

Length of the air column

$$= \frac{3\lambda}{4} = 150 \text{ cm}$$

S16. Ans.(b)



$$T_1 = m_2 g$$

$$T_2 = (m_1 + m_2) g$$

We know velocity $\propto \sqrt{T}$

Also $\lambda \propto \sqrt{T}$

$$\frac{\lambda_1}{\lambda_2} = \frac{\sqrt{T_1}}{\sqrt{T_2}} = \sqrt{\frac{m_2}{m_1 + m_2}}$$

$$\frac{\lambda_2}{\lambda_1} = \sqrt{\frac{m_1 + m_2}{m_2}}$$

S17. Ans.(c)

$$f' = \frac{f_0 v}{v - v_{source}}$$

$$= \frac{800 \times 330}{330 - 15} = 838 \text{ Hz}$$

S18. Ans.(b)

Fundamental frequency of closed organ pipe

$$f = \frac{v}{4l_c}$$

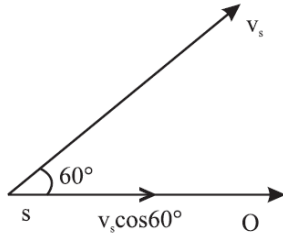
2nd overtone frequency of open organ pipe $f' = \frac{3v}{2l_0}$ Now,

$$\frac{v}{4l_c} = \frac{3v}{2l_0} \Rightarrow l_0 = 6l_c = 6(20 \text{ cm}) = 120 \text{ cm}$$

S19. Ans.(c)

$$f = f_s \left[\frac{v}{v - v_s \cos 60^\circ} \right]$$

$$v = 330 \text{ ms}^{-1}$$



$$f = f_s \left(\frac{v}{v - v_s} \right) = 100 \left(\frac{330}{330 - \frac{19.4}{2}} \right) \approx 103 \text{ Hz}$$

S20. Ans.(d)

$$\text{Frequency COP, } f_n = (2n + 1) \frac{v}{4l}$$

$$\text{For } n = 0, f_0 = 100 \text{ Hz}$$

$$n = 1, f_1 = 300 \text{ Hz}$$

$$n = 2, f_2 = 500 \text{ Hz}$$

$$n = 3, f_3 = 700 \text{ Hz}$$

$$n = 4, f_4 = 900 \text{ Hz}$$

$$n = 5, f_5 = 1100 \text{ Hz}$$

Which are less than 1250 Hz.

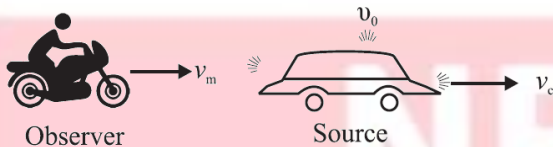
S21. Ans.(a)

$$\text{Total length of string } l = l_1 + l_2 + l_3$$

$$\text{But frequency } \propto \frac{1}{\text{length}}$$

$$\text{Therefore, } \frac{1}{n} = \frac{1}{n_1} + \frac{1}{n_2} + \frac{1}{n_3}$$

S22. Ans.(c)



Here, speed of motorcyclist,

$$v_m = 36 \text{ km hour}^{-1} = 36 \times \frac{5}{18} \text{ ms}^{-1} = 10 \text{ ms}^{-1}$$

Speed for car,

$$v_c = 18 \text{ km hour}^{-1} = 18 \times \frac{5}{18} \text{ ms}^{-1} = 5 \text{ ms}^{-1}$$

Frequency of source, $v_0 = 1392 \text{ Hz}$

Speed of sound, $v = 343 \text{ ms}^{-1}$

The frequency of the honk heard by the motorcyclist is

$$v' = v_0 \left(\frac{v + v_m}{v + v_c} \right) = 1392 \left(\frac{343 + 10}{343 + 5} \right) = \frac{1392 \times 353}{348} = 1412 \text{ Hz}$$

S23. Ans.(a)

Pressure change will be minimum at both open ends

S24. Ans.(b)

Frequency of unknown source = 246 Hz or 254 Hz.

Second harmonic of this source = 492 Hz or 508 Hz which gives 5 beats per second, when sounded with a source of frequency 513 Hz. Therefore unknown frequency = 254 Hz.

S25. Ans.(b)

$$k = \frac{2\pi}{\lambda} = \frac{2\pi}{2\pi} = 1 \text{ and } \omega = 2\pi f = (2\pi) \left(\frac{1}{\pi} \right) = 2$$

So equation of wave

$$y = \sin(kx - \omega t) = \sin(x - 2t)$$